

Instructor Guide

Math and Measurement



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Unit Description

Overview

All jobs require some knowledge of mathematics. Warehousing and distribution are no different. From the receiving dock to the accounting office, working with numbers is important to every aspect of inventory management. Counting the items received, adding and deleting inventory, estimating the amount of space required to store merchandise, interpreting productivity charts, determining shipping costs, and (most importantly) calculating your paycheck all require math skills.

In this module we will review many of the concepts that the participants have learned over the years (and possibly forgotten). We will also advance some concepts that may be new to them. Either way, they will see how each of these concepts is important to warehousing and distribution. Mastering these skills will make their job easier and make them more valuable employees.

Objectives

The information, activities and practice provided during this unit will enable participants to:

1. Perform mathematical computations using whole numbers, fractions, mixed numbers, decimals and percentages.
2. Perform conversions involving fractions, decimals and percentages.
3. Acquire familiarity with measurements of liquid, solid and distance in both English and metric.
4. Calculate an average.
5. Identify common angles.
6. Calculate the perimeter and area of an object.



Materials

Instructor Guide

Participant Guides

Flip Chart or Dry Erase Board

PowerPoint Slides

1. Math and Measurement
2. Objectives
3. Place Value Example 1
4. Place Value Example 2
5. Multiplication Table
6. Examples of Fractions
7. Fractions Shaded
8. Examples of Decimals
9. Reading Decimals
10. Examples of Percents
11. Standards
12. Ruler
13. Earth
14. Metric Place Values
15. Meter Stick
16. Examples of Liquid Standards
17. Equivalents of Liquid Standards
18. Examples of Liquid Metrics



19. Equivalents of Liquid Metrics
20. Pie Graph
21. Bar Graph
22. Line Graph
23. Squares
24. Triangles
25. Circle

Agenda

Introduction	5 minutes
Reviewing the Basics	25 minutes
Fractions	120 minutes
Decimals	30 minutes
Percents	60 minutes
Measurements	120 minutes
Graphs	60 minutes
Geometry	60 minutes
Total	8 hours



Introduction



DISPLAY the slide titled “Math and Measurement.”

WELCOME the participants to the unit and introduce yourself.

Overview



DIRECT the participants to the section titled “Introduction” in their Participant Guides.

EXPLAIN that all jobs require some knowledge of mathematics.

Warehousing and distribution are no different. From the receiving dock to the accounting office, working with numbers is important to every aspect of inventory management. Counting the items received, adding and deleting inventory, estimating the amount of space required to store merchandise, interpreting productivity charts, determining shipping costs, and (most importantly) calculating your paycheck all require math skills.

In this module we will review many of the concepts that the participants have learned over the years (and possibly forgotten). We will also advance some concepts that may be new to them. Either way, they will see how each of these concepts is important to warehousing and distribution. Mastering these skills will make their job easier and make them more valuable employees.



Objectives



DISPLAY the slide titled “Objectives.”

The information, activities and practice provided during this unit will enable participants to:

1. Perform mathematical computations using whole numbers, fractions, mixed numbers, decimals and percentages.
2. Perform conversions involving fractions, decimals and percentages.
3. Acquire familiarity with measurements of liquid, solid and distance in both English and metric.
4. Calculate an average.
5. Identify common angles.
6. Calculate the perimeter and area of an object.



Reviewing the Basics

Whole Numbers



DIRECT the participants to the section titled “Reviewing the Basics” in their Participant Guide.

STATE: “A whole number is a number that has no fractions.”

EXPLAIN that examples of whole numbers are 0, 5, 46, 132, 2879, and 36821.

CONTINUE BY SAYING that while the digits 0 through 9 are included in all of these numbers, the numbers each mean something different because the digits are in different places. Each place has a different value.

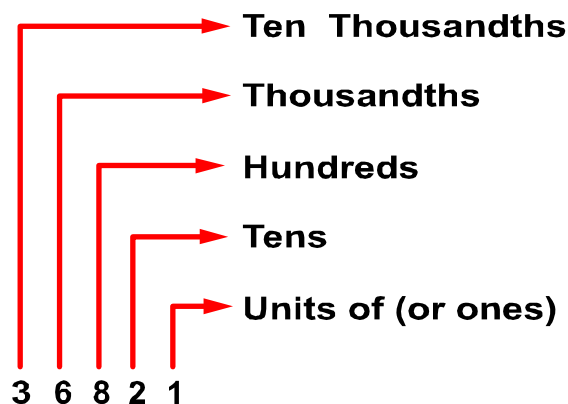
Place Values

STATE: “The number 36821 has five different digits, each having a place value.”



DISPLAY the slide titled “Place Values Example 1.”

EXPLAIN that in this example, there are 3 ten thousands, 6 thousands, 8 hundreds, 2 tens, and one unit.

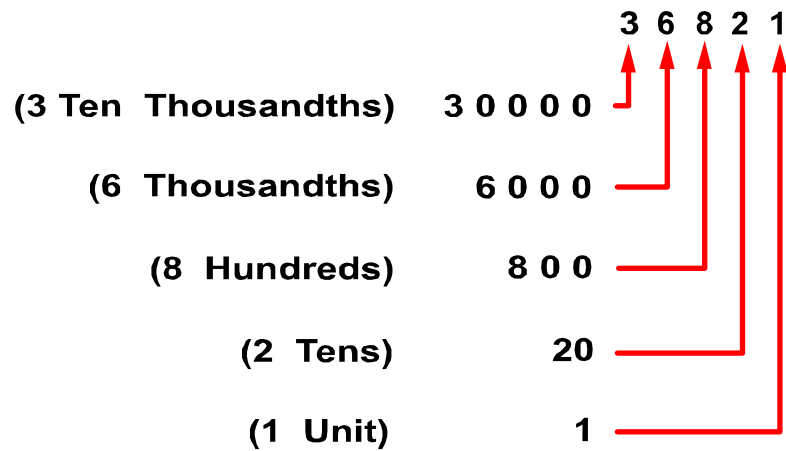


Place Values Example 1



DISPLAY the slide titled “Place Values Example 2.”

STATE: “When they are combined (added), we have the number thirty-six thousand, eight hundred and twenty-one.”



Place Values Example 2



Adding Whole Numbers

STATE: “Addition is the process of bringing together two or more numbers to make a larger number. The addition process is usually denoted by a plus (+) sign.”

EXPLAIN that adding single-digit numbers is easy. We all know that $4 + 2 = 6$. We can do that in our heads.

CONTINUE BY SAYING that adding larger numbers becomes more difficult. To add 4352 and 217, most of us would have to use a calculator. Unfortunately, we don’t always have a calculator handy so we must resort to pencil and paper.

EXPLAIN that using this method, we must first align the numbers so that the units are in one column, the tens in one column, etc. We then add the columns beginning with the units column and moving left.



WRITE the addition example on the flip chart.

④
$$\begin{array}{r} 4352 \\ + 217 \\ \hline 569 \end{array}$$
 Add the Hundreds Column

⑤
$$\begin{array}{r} 4352 \\ + 217 \\ \hline 4569 \end{array}$$
 Add the Thousands Column

Carrying

STATE: “The addition process is fairly simple until the total for a column exceeds 9. When that occurs, we must ‘carry’ the excess to the next column.”



WRITE the Carrying example on the flip chart.

①
$$\begin{array}{r} 6875 \\ + 348 \\ \hline 3 \end{array}$$
 Align & add the Units column

②
$$\begin{array}{r} 1 \\ 6875 \\ + 348 \\ \hline 3 \end{array}$$
 Carry the “1” over to the Tens column

③
$$\begin{array}{r} 1 \\ 6875 \\ + 348 \\ \hline 23 \end{array}$$
 Add the Tens column

④
$$\begin{array}{r} 11 \\ 6875 \\ + 348 \\ \hline 23 \end{array}$$
 Carry the “1” over to the Hundreds column

⑤
$$\begin{array}{r} 11 \\ 6875 \\ + 348 \\ \hline 223 \end{array}$$
 Add the Hundreds column

⑥
$$\begin{array}{r} 111 \\ 6875 \\ + 348 \\ \hline 223 \end{array}$$
 Carry the “1” over to the Thousands column

⑦
$$\begin{array}{r} 111 \\ 6875 \\ + 348 \\ \hline 7223 \end{array}$$
 Add the Thousands column



Subtracting Whole Numbers

STATE: “Subtraction is the process of finding the difference between two numbers. The subtraction process is usually denoted by a minus (–) sign.”

EXPLAIN that , subtracting small numbers is simple. It is easy to determine that $6 - 2 = 4$. We give very little thought to it.

CONTINUE BY SAYING that subtracting larger numbers is a bit more involved. Subtracting 3412 from 8618 would require some thought. Without a calculator, we will again resort to pencil and paper.

EXPLAIN that the subtraction process begins by placing the smaller number below the larger one. Then, just as we did in addition, we align the numbers to the right so that the units are in one column, the tens in one column, etc. Starting in the units column and moving left, we subtract the bottom number from the top number.



WRITE the Subtraction example on the flip chart.

①
$$\begin{array}{r} 8618 \\ - 3412 \\ \hline \end{array}$$
 Place smaller number under the larger number & align

②
$$\begin{array}{r} 8618 \\ - 3412 \\ \hline 6 \end{array}$$
 Subtract the Units Column

③
$$\begin{array}{r} 8618 \\ - 3412 \\ \hline 06 \end{array}$$
 Subtract the Tens Column

④
$$\begin{array}{r} 8618 \\ - 3412 \\ \hline 206 \end{array}$$
 Subtract the Hundreds Column

⑤
$$\begin{array}{r} 8618 \\ - 3412 \\ \hline 5206 \end{array}$$
 Subtract the Thousands Column



“Borrowing”

CONTINUE BY SAYING that the subtraction process is fairly simple until a bottom digit in one of the columns is greater than the top digit in that column. When this occurs, we must “borrow” from the top digit in the next column.



WRITE the Borrowing example on the flip chart.

①

$$\begin{array}{r} 2354 \\ - 796 \\ \hline \end{array}$$

Align

②

$$\begin{array}{r} 4 \\ 23\cancel{5}4 \\ - 796 \\ \hline 8 \end{array}$$

Borrow “1” from the Tens Column and subtract

③

$$\begin{array}{r} 24 \\ 2\cancel{3}\cancel{5}4 \\ - 796 \\ \hline 58 \end{array}$$

Borrow “1” from the Hundreds Column and subtract

④

$$\begin{array}{r} 124 \\ \cancel{2}\cancel{3}\cancel{5}4 \\ - 796 \\ \hline 558 \end{array}$$

Borrow “1” from the Thousands Column and subtract



“Borrowing” Across the Zero

EXPLAIN that once it is understood, borrowing appears to be simple process until we attempt to borrow from zero. After all, you can’t borrow from “nothing.” When that occurs we must “borrow” across the zero.



WRITE the Borrowing across Zeros example on the flip chart.

①
$$\begin{array}{r} 6000 \\ - 547 \\ \hline ? \end{array}$$
 Align & Subtract Units Column
(Cannot subtract 7 from 0)

②
$$\begin{array}{r} 5 \\ \cancel{6}000 \\ - 547 \\ \hline \end{array}$$
 Borrow “1” from the Thousands Column and subtract

③
$$\begin{array}{r} 59 \\ \cancel{6}\cancel{0}00 \\ - 547 \\ \hline \end{array}$$
 Borrow “1” from the Hundreds Column and subtract

④
$$\begin{array}{r} 599 \\ \cancel{6}\cancel{0}\cancel{0}0 \\ - 547 \\ \hline \end{array}$$
 Borrow “1” from the Tens Column and subtract

⑤
$$\begin{array}{r} 599 \\ \cancel{6}\cancel{0}\cancel{0}0 \\ - 547 \\ \hline 5453 \end{array}$$
 Subtract as usual



Multiplying Whole Numbers

STATE: “Multiplication is the process of adding a number to itself as many times as indicated by a second number. A ‘times’ (\times) sign denotes the multiplication process.”

EXPLAIN that multiplying 4 times 2 (4×2) is the same as adding 4 two times ($4 + 4$). They both equal 8.

CONTINUE BY SAYING that multiplying 6 times 7 (6×7) is the same as adding 6 seven times ($6 + 6 + 6 + 6 + 6 + 6 + 6$). They both equal 42.

Multiplication Table

STATE: “Adding a long list of numbers is difficult. It is easier to use a multiplication table.”

EXPLAIN that a multiplication table is a list of answers for multiplying any two numbers (in this case, 0 through 12).

	0	1	2	3	4	5	6	7	8	9	10	11	12
0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	1	2	3	4	5	6	7	8	9	10	11	12
2	0	2	4	6	8	10	12	14	16	18	20	22	24
3	0	3	6	9	12	15	18	21	24	27	30	33	36
4	0	4	8	12	16	20	24	28	32	36	40	44	48
5	0	5	10	15	20	25	30	35	40	45	50	55	60
6	0	6	12	18	24	30	36	42	48	54	60	66	72
7	0	7	14	21	28	35	42	49	56	63	70	77	84
8	0	8	16	24	32	40	48	56	64	72	80	88	96
9	0	9	18	27	36	45	54	63	72	81	90	99	108
10	0	10	20	30	40	50	60	70	80	90	100	110	120
11	0	11	22	33	44	55	66	77	88	99	110	121	132
12	0	12	24	36	48	60	72	84	96	108	120	132	144

Multiplication Table



STATE: “To use a multiplication table, simply locate the point where the two numbers being multiplied intersect.”

Example

$$6 \times 8 = ?$$



DISPLAY the slide “Multiplication Table”

EXPLAIN each step of using the Multiplication Table.

Step 1: From the 6 in the left column, draw a line to the right.

Step 2: From the 8 in the top row, draw a line downward.

STATE: “We see that the lines cross at 48. ($6 \times 8 = 48$.)”

EXPLAIN that while the multiplication table makes it easy to multiply small numbers (less than 12), it is just as useful when multiplying larger numbers.

NOTE: Throughout this module the participant may use the multiplication table.



WRITE the Multiplying example on the flip chart.

①

$$\begin{array}{r} 42 \\ \times 31 \\ \hline \end{array}$$

Align the two numbers

②

$$\begin{array}{r} 42 \\ \times 31 \\ \hline 2 \end{array}$$

Multiply the units in the bottom number by the units in the top

③

$$\begin{array}{r} 42 \\ \times 31 \\ \hline 42 \end{array}$$

Multiply the units in the bottom number by the tens in the top

④

$$\begin{array}{r} 42 \\ \times 31 \\ \hline 42 \\ 6 \end{array}$$

Multiply the tens in the bottom number by the units in the top

⑤

$$\begin{array}{r} 42 \\ \times 31 \\ \hline 42 \\ 126 \end{array}$$

Multiply the tens in the bottom number by the tens in the top

⑥

$$\begin{array}{r} 42 \\ \times 31 \\ \hline 42 \\ 126 \\ \hline 1302 \end{array}$$

Partial answers

Add the partial answers

Carrying

STATE: “Carrying when multiplying is very similar to carry when adding.”



WRITE the Multiplication Carrying example on the flip chart.

①

$$\begin{array}{r} 73 \\ \times 68 \\ \hline \end{array}$$

Multiply the units in the bottom number by the units in the top number

$$\begin{array}{r} 73 \\ \times 68 \\ \hline 24 \end{array}$$

Carry the "2" over to the Tens Column

②

$$\begin{array}{r} 73 \\ \times 68 \\ \hline 5824 \end{array}$$

Multiply the units in the bottom number by the tens in the top number and add the "carry"

③

$$\begin{array}{r} 73 \\ \times 68 \\ \hline 584 \end{array}$$

Multiply the tens in the bottom number by the units in the top number

$$\begin{array}{r} 73 \\ \times 68 \\ \hline 584 \\ 18 \end{array}$$

Carry the "1" over to the Hundreds Column

④

$$\begin{array}{r} 73 \\ \times 68 \\ \hline 584 \\ 438 \end{array}$$

Multiply the tens in the bottom number by the tens in the top number and add the "carry"

⑤

$$\begin{array}{r} 73 \\ \times 68 \\ \hline 584 \\ 438 \\ \hline 4964 \end{array}$$

Partial answers

Add the partial answers

STATE: “Be sure that you multiply first then add the number being carried.”



Dividing Whole Numbers

STATE: “Division is the process of finding out how many times one number is contained in another. The division process is usually denoted by either of two “divided by” signs: \div and $/$.”

EXPLAIN that most of us can quickly determine that there are 20 nickels in a dollar. In other words, 5 is contained in 100 twenty times. We did this by dividing 100 cents by 5 cents.

$$100 \div 5 = 20$$



WRITE “ $100 \div 5 = 20$ ” on the flip chart.

STATE: “The same division problem can be written in another way.”



WRITE the example on the flip chart.

$$\begin{array}{r} 20 \\ 5 \overline{)100} \end{array}$$

EXPLAIN that this method of writing division problems will be useful when we have larger numbers.



Dividing Small Numbers

STATE: “The Multiplication Table is a handy tool to use when dividing smaller numbers.”

Example

$$48 \div 6 = ?$$

EXPLAIN each step of using the Multiplication Table for division.

Step 1: From the 6 in the left column, draw a line to the right until you reach the 48.

Step 2: From the 48, draw a line to the top row.

STATE: “We see that the line stops at 8. ($48 \div 6 = 8$.)”



Dividing with a Remainder

STATE: “The previous example had an answer that came out evenly...that is, without any amount remaining. Many division problems have a remainder.”

EXPLAIN that the Multiplication Table is still a handy tool to use when dividing smaller numbers...with or without remainders.

Example

$$58 \div 7 = ?$$

EXPLAIN each step of using the Multiplication Table for division with a remainder.

Step 1: Using the Multiplication Table, find the 7 on the left-hand column.

Step 2: Follow the row to the right until you find a number as close as possible to 58 without going over 58. It should be 56.

Step 3: Go up the column until you find the number on the top row. It should be 8.

Step 4: Subtract 56 from 58 to determine the remainder of 2.

STATE: “Completing the process, we see that $58 \div 7 = 8$ with a remainder of 2.”

EXPLAIN that the answer may be written: 8 R 2.

Dividing Larger Numbers with Remainders

STATE: “To divide larger numbers, we can still use the Multiplication Table, but we must simplify the large number into smaller ones. To do this, it is easier to write the division problem in a different manner.”



WRITE the Dividing example on the flip chart.

①
$$\begin{array}{r} 47 \overline{)1534} \end{array}$$
 Estimate how many times 47 goes into 153

②
$$\begin{array}{r} 3 \\ 47 \overline{)1534} \\ \underline{141} \end{array}$$
 Multiply

③
$$\begin{array}{r} 3 \\ 47 \overline{)1534} \\ \underline{141} \\ 12 \end{array}$$
 Subtract

④
$$\begin{array}{r} 3 \\ 47 \overline{)1534} \\ \underline{141} \downarrow \\ 124 \end{array}$$
 Bring down the 4

⑤
$$\begin{array}{r} 32 \\ 47 \overline{)1534} \\ \underline{141} \downarrow \\ 124 \end{array}$$
 Estimate how many times 47 goes into 124

⑥
$$\begin{array}{r} 32 \\ 47 \overline{)1534} \\ \underline{141} \\ 124 \\ 94 \end{array}$$
 Multiply

⑦
$$\begin{array}{r} 32 \\ 47 \overline{)1534} \\ \underline{141} \\ 124 \\ \underline{94} \\ 30 \end{array}$$
 Subtract

⑧
$$32 \text{ r } 30$$
 Final Answer with Remainder



Progress Check #1



DIRECT the participants to the section titled “Progress Check # 1” in their Participant Guide.

ALLOW them enough time to complete the Progress Check and then review the answers.

1. Add the following:

a. $57 + 48 = \underline{105}$

b. $341 + 879 + 564 = \underline{1784}$

c. $4682 + 3579 + 1245 + 9753 = \underline{19259}$

2. Subtract the following:

a. $52 - 28 = \underline{24}$

b. $457 - 398 = \underline{59}$

c. $10000 - 2648 = \underline{7352}$

3. Multiply the following:

a. $4 \times 8 = \underline{32}$

b. $66 \times 78 = \underline{5148}$

c. $253 \times 93 = \underline{23529}$

4. Divide the following:

a.
$$\begin{array}{r} 9 \\ 7 \overline{)63} \\ \underline{63} \\ 0 \end{array}$$

b.
$$\begin{array}{r} 14 \\ 23 \overline{)322} \\ \underline{23} \\ 92 \\ \underline{92} \\ 0 \end{array}$$

c.
$$\begin{array}{r} 74r33 \\ 342 \overline{)25341} \\ \underline{2394} \\ 1402 \\ \underline{1368} \\ 33 \end{array}$$



5. The Receiving Department accepted 75 cases of “Birds of the World” alarm clocks. There are 24 clocks in each case. How many clocks were received?

1800

6. Prior to this delivery, there were 30 cases already in the warehouse. What is the total number of clocks in the warehouse after receipt of the delivery?

2520

7. The Shipping Department must ship an equal number of clocks to 15 stores. If all the clocks are to be shipped, how many cases must be shipped to each store?

7

8. How many clocks will each store receive?

168



Fractions



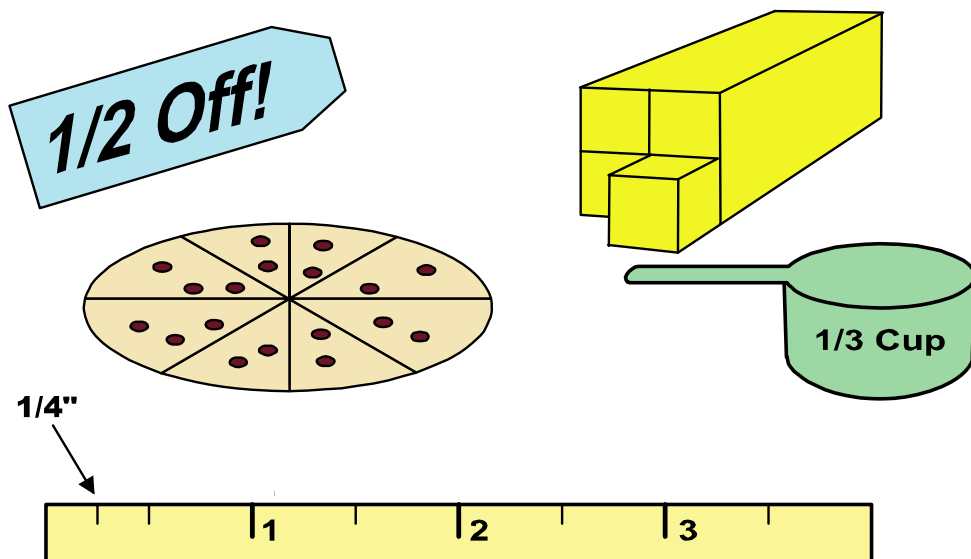
DIRECT the participants to the section titled “Fractions” in their Participant Guides.

STATE: “A fraction is a way of expressing a part of a whole.”

EXPLAIN that we deal with fractions all of the time. Department stores have “half-off” sales. Recipes call for $\frac{1}{3}$ cup of sugar or $\frac{1}{4}$ pound of margarine. We travel $\frac{4}{10}$ of a mile to pick up a pizza cut into eight slices. (Each slice is $\frac{1}{8}$ of the whole pizza.) We measure $\frac{1}{16}$ of an inch on a ruler. The list is endless.



DISPLAY the slide titled “Examples of Fractions”



Examples of Fractions

EXPLAIN that there are two parts to a fraction. The top number and the bottom number.

CONTINUE BY SAYING that the bottom number tells us the total number of parts in the whole.

EXPLAIN that the top number tells us the number of parts we are talking about.

Proper Fractions



DISPLAY the slide titled, “Fractions Shaded.”

DISCUSS each of the examples:

Examples:

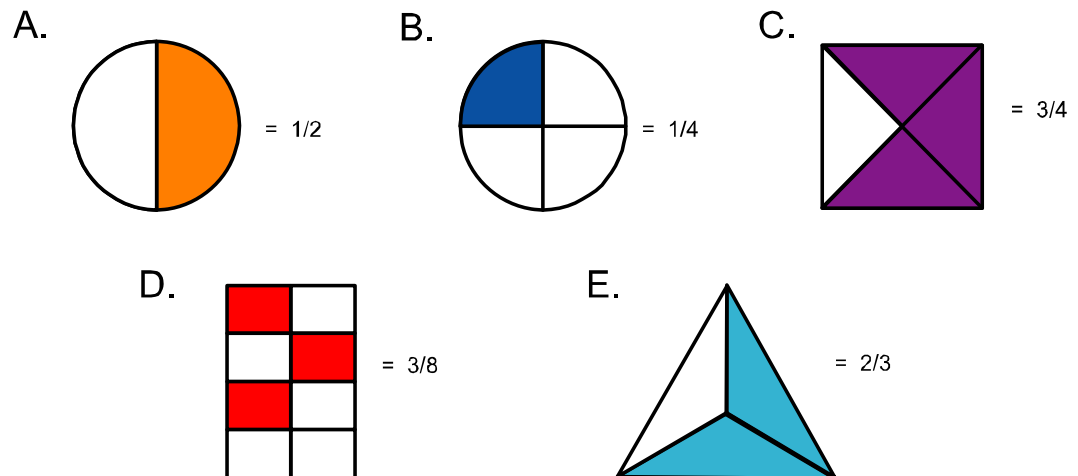
In illustration “A”, the circle has two parts. One part is shaded. The fraction $\frac{1}{2}$ tells you how much of the circle is shaded.

In illustration “B”, the circle has four parts. One part is shaded. The fraction $\frac{1}{4}$ tells you how much of the circle is shaded.

In illustration “C”, the square has four parts. Three parts are shaded. The fraction $\frac{3}{4}$ tells you how much of the circle is shaded.

In illustration “D”, the rectangle has eight parts. Three parts are shaded. The fraction $\frac{3}{8}$ tells you how much of the circle is shaded.

In illustration “E”, the triangle has three parts. Two parts are shaded. The fraction $\frac{2}{3}$ tells you how much of the circle is shaded.



Fractions Shaded

STATE: “These fractions are known as proper fractions because the top number is smaller than the bottom number.”



Reducing Fractions

STATE: “Sometimes fractions can be a bit too large to handle easily. When this occurs, we try to reduce the fraction to make it easier.”

EXPLAIN that reducing a fraction means to write the fraction using smaller numbers without changing the fraction’s value.

STATE: “Example #1: A recipe takes 6 eggs. That means we would need $\frac{6}{12}$ of a dozen of eggs. Six-twelfths is a bit cumbersome. Let’s reduce the fraction by finding a number that divides into both the top and bottom numbers evenly. In this case, 6 will divide into both numbers.”



WRITE the example on the flip chart.

EXPLAIN each step of the process.

$$\frac{6 \div 6}{12 \div 6} = \frac{1}{2}$$

STATE: “After dividing both numbers by six, we have reduced the fraction to $\frac{1}{2}$... a much easier fraction to handle. Moreover, we have not changed its value. Six eggs are half a dozen.”

STATE: “Example #2: A dollar is equal to one hundred pennies. A dime is equal to ten pennies. Therefore, a dime is $\frac{10}{100}$ of a dollar. Let’s reduce the fraction. Ten will divide into both numbers.”



WRITE the example on the flip chart.

EXPLAIN each step of the process.

$$\frac{10 \div 10}{100 \div 10} = \frac{1}{10}$$

STATE: “As you can see, we have reduced $\frac{10}{100}$ to $\frac{1}{10}$, an easier number to handle, without changing its value. After all, a dime is one-tenth of a dollar.”



Mixed Numbers

STATE: “A mixed number is a combination of a whole number and a fraction.

EXPLAIN that $2\frac{1}{3}$, $5\frac{3}{4}$, and $4\frac{5}{6}$ are examples of mixed numbers.

CONTINUE BY SAYING that mixed numbers can be converted to fractions by a simple process.

Example

Convert $4\frac{2}{3}$ to a fraction.



WRITE the example on the flip chart.

$$4\frac{2}{3} = \overset{\textcircled{1}}{\frac{(4 \times 3) + 2}{3}} = \overset{\textcircled{2}}{\frac{(12) + 2}{3}} = \overset{\textcircled{3}}{\frac{14}{3}}$$

EXPLAIN each step of the process.

Step 1: Multiply the bottom number (3) by the whole number (4).
 $3 \times 4 = 12$

Step 2: Add the top number (2).
 $2 + 12 = 14$

Step 3: Write the sum over the bottom number: $\frac{14}{3}$.



Improper Fractions

STATE: “As you saw in the previous example, there may be times when the top number of a fraction is equal to or larger than the bottom number. In those cases, the fractions are known as improper fractions.”

EXPLAIN that $\frac{9}{8}$, $\frac{5}{4}$, and $\frac{6}{3}$ are examples of improper fractions.

CONTINUE BY SAYING that an improper fraction can be converted into a whole or mixed number without changing its value.

STATE: “Example #1: Convert $\frac{7}{7}$ to a whole number.”

EXPLAIN that $\frac{7}{7}$ can be converted to a whole number by dividing the bottom number into the top number.



WRITE the example on the flip chart.

EXPLAIN each step of the process.

$$7 \div 7 = 1$$

STATE: “Example #2: Convert $\frac{12}{8}$ into a mixed number.”



WRITE the example on the flip chart.

①②③

$$\begin{array}{r} 1 \\ 8 \overline{) 12} \\ \underline{8} \\ 4 \end{array}$$

$$\begin{array}{r} 4 \div 4 = 1 \\ 8 \div 4 = 2 \end{array}$$

$$1 \frac{1}{2}$$



EXPLAIN each step of the process.

Step 1: Divide the bottom number (8) into the top number (12).

Step 2: Write the remainder (4) over the bottom number (8).

Step 3: Reduce the fraction ($\frac{4}{8}$) to its lowest terms.
(Divide both numbers by 4).

STATE: “We see that $\frac{12}{8}$ equals $1 \frac{1}{2}$.”

Whole Numbers as Fractions

STATE: “Any whole number can be written as an improper fraction with the bottom number as 1.”



WRITE the example on the flip chart.

$$5 = \frac{5}{1} \quad 9 = \frac{9}{1} \quad 12 = \frac{12}{1} \quad 25 = \frac{25}{1}$$

EXPLAIN each step of the process.



Adding and Subtracting Fractions

STATE: “The key to addition and subtraction of fractions is to make the bottom number the same on all of the fractions.”

Like Fractions

EXPLAIN that if the bottom numbers are already the same, addition is easy. We simply add the top numbers and reduce if necessary.

STATE: “Example: $\frac{3}{4} + \frac{1}{4} = ?$ ”



WRITE the example on the flip chart.

$$\begin{array}{r} \textcircled{1} \quad \textcircled{2} \quad \textcircled{3} \\ \frac{3}{4} \\ + \frac{1}{4} \\ \hline \frac{4}{4} = 4 \div 4 = 1 \end{array}$$

EXPLAIN each step of the process.

Step 1: Add the top numbers. $3 + 1 = 4$

Step 2: Place the sum over the bottom number. $\frac{4}{4}$

Step 3: Reduce. (Divide the top number by the bottom number).
 $4 \div 4 = 1$

STATE: “We see that $\frac{3}{4} + \frac{1}{4} = 1$.”



Unlike Fractions

STATE: “If the bottom numbers are different, it’s a little trickier to add. We must convert the fractions so that the bottom numbers are the same without changing the value of the fractions.”

STATE: “Example: $\frac{1}{2} + \frac{3}{8} = ?$ ”



WRITE the example on the flip chart.

$$\begin{array}{r} \textcircled{1} \qquad \textcircled{2} \qquad \textcircled{3} \\ \frac{1}{2} = \frac{1 \times 4}{2 \times 4} = \frac{4}{8} \\ + \frac{1}{4} = \frac{3}{8} = \frac{3}{4} \\ \hline \frac{7}{8} \end{array}$$

EXPLAIN each step of the process.

Step 1: Since 2 divides evenly into 8, we will use 8 as the bottom numbers on both fractions.

Step 2: Divide the 2 into the 8. ($8 \div 2 = 4$)

Step 3: Multiply the 1 by the 4. ($1 \times 4 = 4$)

Step 4: Place the 4 over 8. $\frac{4}{8}$

EXPLAIN that we have converted $\frac{1}{2}$ to $\frac{4}{8}$ without changing the value of the fraction.”

Step 5: Add the top numbers. ($4 + 3 = 7$)

Step 6: Place the sum (7) over 8.

STATE: “We see that $\frac{1}{2} + \frac{3}{8} = \frac{7}{8}$.”



Mixed Numbers

STATE: “Adding or subtracting mixed numbers uses the same process.”

STATE: “Example: $2\frac{5}{6} - 1\frac{2}{3} = ?$ ”



WRITE the example on the flip chart.

$$\begin{array}{r} \textcircled{1} \qquad \textcircled{2} \qquad \textcircled{3} \\ 2\frac{5}{6} = 2\frac{5}{6} = 2\frac{5}{6} \\ - 1\frac{2}{3} = 1\frac{2 \times 2}{3 \times 2} = 1\frac{4}{6} \\ \hline 1\frac{1}{6} \end{array}$$

EXPLAIN each step of the process.

Step 1: Since 3 divides evenly into 6, we will use 6 as the bottom numbers on both fractions.

Step 2: Divide the 3 into the 6. ($6 \div 3 = 2$)

Step 3: Multiply the bottom 3 by 2. ($3 \times 2 = 6$)

Step 4: Multiply the top 2 by 2. ($2 \times 2 = 4$)

Step 4: Place the 4 over the 6.

Step 5: Now that the bottom numbers of the fractions are the same, we simply subtract the top numbers. $5 - 4 = 1$

Step 6: Subtract the whole numbers. $2 - 1 = 1$

STATE: “We see that $2\frac{5}{6} - 1\frac{2}{3}$ equals $1\frac{1}{6}$.”



Borrowing

STATE: “There may be times when you need to subtract mixed numbers, such as when the bottom fraction is larger than the top fraction. To resolve this situation, we borrow from the whole number.”

EXPLAIN that we do this by converting part of the whole number into a fraction.

STATE: “Example: $3\frac{1}{4} - 2\frac{3}{4} = ?$ ”

EXPLAIN that since $\frac{3}{4}$ is larger than $\frac{1}{4}$, we must borrow from the 3.



WRITE the example on the flip chart.

$$\begin{array}{r} \textcircled{1} \qquad \qquad \textcircled{2} \qquad \qquad \textcircled{3} \quad \textcircled{4} \quad \textcircled{5} \\ 3\frac{1}{4} = 2\frac{4}{4} + \frac{1}{4} = 2\frac{5}{4} \\ - 2\frac{3}{4} = 2\frac{3}{4} = 2\frac{3}{4} \\ \hline \end{array}$$
$$\frac{2 \div 2}{4 \div 2} = \frac{1}{2}$$

EXPLAIN each step of the process.

Step 1: Subtract 1 from the top whole number 3. ($3 - 1 = 2$)

Step 2: Convert the 1 into fourths. $1 = \frac{4}{4}$

Step 3: Add the $\frac{4}{4}$ to the $\frac{1}{4}$. ($\frac{4}{4} + \frac{1}{4} = \frac{5}{4}$)

Step 4: Subtract the whole numbers. $2 - 2 = 0$

Step 5: Subtract the fractions. $\frac{5}{4} - \frac{3}{4} = \frac{2}{4}$

Step 6: Reduce the fraction. $\frac{2}{4} = \frac{1}{2}$



Multiplying Fractions

STATE: “Multiplying fractions means finding part of a fraction (e.g. one-half of one-tenth). Therefore, the answer will be smaller than both of the two fractions you multiplied.”

EXPLAIN that in the example above, one-half of one-tenth is one-twentieth. One-twentieth is smaller than both one-half and one-tenth.

CONTINUE BY SAYING that multiplying fractions is a simple process of multiplying the top numbers, then multiplying the bottom numbers.



WRITE the example on the flip chart.

Examples:

	①	②	③
a.	$\frac{1}{3}$	$\times \frac{2}{5}$	$= \frac{1 \times 2}{3 \times 5} = \frac{2}{15}$
b.	$\frac{3}{4}$	$\times \frac{5}{9}$	$= \frac{3 \times 5}{4 \times 9} = \frac{15}{36}$
c.	$\frac{1}{2}$	$\times \frac{4}{7}$	$= \frac{1 \times 4}{2 \times 7} = \frac{4}{14} = \frac{2}{7}$

EXPLAIN each step of the process.



Multiplying Mixed Numbers

STATE: “Multiplying mixed numbers is almost as easy. To multiply mixed numbers we must change the mixed numbers to improper fractions. Then we follow the same process as multiplying fractions.”

STATE: “Example: $4\frac{2}{3} \times 3\frac{1}{6} = ?$ ”



WRITE the example on the flip chart.

$$\begin{array}{cccccc} \textcircled{1} & & \textcircled{2} & & \textcircled{3} & & \textcircled{4} & & \textcircled{5} & & \textcircled{6} \\ 4\frac{2}{3} \times 3\frac{1}{6} = \frac{14}{3} \times \frac{19}{6} = \frac{14 \times 19}{3 \times 6} = \frac{266}{18} = 14\frac{14}{18} = 14\frac{7}{9} \end{array}$$

EXPLAIN each step of the process.



Dividing Fractions

STATE: “Dividing fractions is slightly more difficult. When dividing by a fraction, we must invert the second fraction and then multiply.”

STATE: “Example #1: $\frac{5}{6} \div \frac{3}{8} = ?$ ”



WRITE the example on the flip chart.

①

$$\frac{5}{6} \div \frac{3}{8} =$$

②

$$\frac{5}{6} \div \frac{8}{3} =$$

Invert

③

$$\frac{5}{6} \times \frac{8}{3} =$$

Multiply

④

⑤

⑥

⑦

$$\frac{5}{6} \times \frac{8}{3} = \frac{5 \times 8}{6 \times 3} = \frac{40}{18} = 2\frac{4}{18} = 2\frac{2}{9}$$

EXPLAIN each step of the process.



Dividing Mixed Numbers

EXPLAIN that dividing mixed numbers requires converting the mixed numbers to improper fractions then inverting and multiplying smaller fractions.

STATE: “Example #2: $3\frac{2}{3} \div 1\frac{4}{5} = ?$ ”



WRITE the example on the flip chart.

$$\begin{array}{l} \textcircled{1} \qquad \qquad \qquad \textcircled{2} \\ 3\frac{2}{3} \div 1\frac{4}{5} = \frac{11}{3} \div \frac{9}{5} = \\ \textcircled{3} \qquad \qquad \qquad \text{Invert} \\ \frac{11}{3} \div \frac{5}{9} = \\ \text{Multiply} \\ \textcircled{4} \qquad \qquad \qquad \textcircled{5} \qquad \textcircled{6} \qquad \textcircled{7} \\ \frac{11}{3} \times \frac{5}{9} = \frac{11 \times 5}{3 \times 9} = \frac{55}{27} = 2\frac{1}{27} \end{array}$$

EXPLAIN each step of the process.



Progress Check # 2



DIRECT the participants to the section titled “Progress Check # 2” in their Participant Guide.

ALLOW them enough time to complete the Progress Check and then review the answers.

1. Reduce the following fractions to their lowest terms:

a. $\frac{6}{8}$	b. $\frac{5}{10}$	c. $\frac{3}{9}$	d. $\frac{15}{45}$
$\frac{3}{4}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{3}$

2. Convert the following mixed numbers to fractions:

a. $1\frac{5}{6}$	b. $3\frac{7}{8}$	c. $4\frac{1}{2}$	d. $5\frac{3}{4}$
$\frac{11}{6}$	$\frac{31}{8}$	$\frac{9}{2}$	$\frac{23}{4}$

3. Convert the following improper fractions to mixed numbers:

a. $\frac{13}{7}$	b. $\frac{8}{3}$	c. $\frac{27}{12}$	d. $\frac{37}{4}$
$1\frac{6}{7}$	$2\frac{2}{3}$	$2\frac{1}{4}$	$9\frac{1}{4}$

4. Add the following fractions:

a. $\frac{5}{8}$	b. $\frac{7}{16}$	c. $\frac{5}{6}$	d. $\frac{4}{12}$
$+\frac{2}{8}$	$+\frac{9}{16}$	$+\frac{1}{2}$	$+\frac{2}{3}$
$\frac{7}{8}$	1	$1\frac{1}{3}$	1



5. Subtract the following fractions:

$$\begin{array}{r} \text{a. } \frac{11}{32} \\ - \frac{6}{32} \\ \hline \frac{5}{32} \end{array}$$

$$\begin{array}{r} \text{b. } \frac{7}{8} \\ - \frac{1}{8} \\ \hline \frac{3}{4} \end{array}$$

$$\begin{array}{r} \text{c. } \frac{3}{4} \\ - \frac{1}{3} \\ \hline \frac{5}{12} \end{array}$$

$$\begin{array}{r} \text{d. } \frac{3}{5} \\ - \frac{3}{15} \\ \hline \frac{3}{4} \end{array}$$

6. Add the following mixed numbers:

$$\begin{array}{r} \text{a. } 1\frac{1}{8} \\ + 4\frac{2}{8} \\ \hline 5\frac{3}{8} \end{array}$$

$$\begin{array}{r} \text{b. } 2\frac{1}{3} \\ + 5\frac{1}{15} \\ \hline 7\frac{6}{15} \end{array}$$

$$\begin{array}{r} \text{c. } 3\frac{7}{8} \\ + 3\frac{7}{8} \\ \hline 7\frac{3}{4} \end{array}$$

$$\begin{array}{r} \text{d. } 6\frac{13}{27} \\ + 7\frac{5}{9} \\ \hline 14\frac{1}{27} \end{array}$$

7. Subtract the following mixed numbers:

$$\begin{array}{r} \text{a. } 2\frac{2}{8} \\ - 1\frac{1}{8} \\ \hline 1\frac{1}{8} \end{array}$$

$$\begin{array}{r} \text{b. } 3\frac{1}{4} \\ - 1\frac{3}{12} \\ \hline 2 \end{array}$$

$$\begin{array}{r} \text{c. } 4\frac{1}{6} \\ - 2\frac{5}{6} \\ \hline 1\frac{1}{3} \end{array}$$

$$\begin{array}{r} \text{d. } 5\frac{13}{35} \\ - 3\frac{3}{7} \\ \hline 1\frac{33}{35} \end{array}$$

8. Multiply the following fractions:

$$\begin{array}{r} \text{a. } \frac{4}{5} \times \frac{3}{8} \\ \hline \frac{3}{10} \end{array}$$

$$\begin{array}{r} \text{b. } \frac{4}{9} \times \frac{2}{3} \\ \hline \frac{8}{27} \end{array}$$

$$\begin{array}{r} \text{c. } \frac{1}{6} \times \frac{1}{4} \\ \hline \frac{1}{24} \end{array}$$



9. Multiply the following mixed numbers:

a. $2\frac{1}{8} \times 1\frac{2}{3}$
 $3\frac{13}{24}$

b. $3\frac{2}{3} \times 5\frac{1}{6}$
 $18\frac{17}{18}$

10. Divide the following fractions:

a. $\frac{1}{3} \div \frac{1}{3}$
 1

b. $\frac{3}{5} \div \frac{2}{3}$
 $\frac{9}{10}$

11. Divide the following mixed numbers:

a. $1\frac{1}{2} \div 2\frac{1}{3}$
 $\frac{9}{14}$

b. $4\frac{2}{9} \div 2\frac{1}{8}$
 $1\frac{151}{153}$

12. During the annual inventory it was learned that there were several partial cases of unsold books. You have been directed to consolidate all of the books into one shipment for donation to charity. You must calculate how many total cases the charity will receive. Below are the quantities by book title:

Title 1: $2\frac{1}{2}$ cases

Title 2: $3\frac{3}{4}$ cases

Title 3: $4\frac{2}{3}$ cases

Title 4: $1\frac{1}{6}$ cases

Title 5: 3 cases

Total: $15\frac{1}{2}$ cases



Decimals



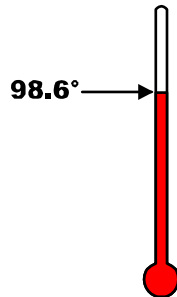
DIRECT the participants to the section titled “Decimals” in their Participant Guides.



DISPLAY slide titled “Examples of Decimals.”

STATE: “Just as with fractions, we work with decimal numbers everyday without realizing it. A body temperature of 98.6 is considered normal. We pay \$1.29 for a gallon of gasoline. We traveled 12.4 miles to work.”

EXPLAIN that numbers like 98.6, 1.29 and 12.4 are decimals.



FasTrak Gasoline	
Regular	1.29
Plus	1.39
Super	1.49

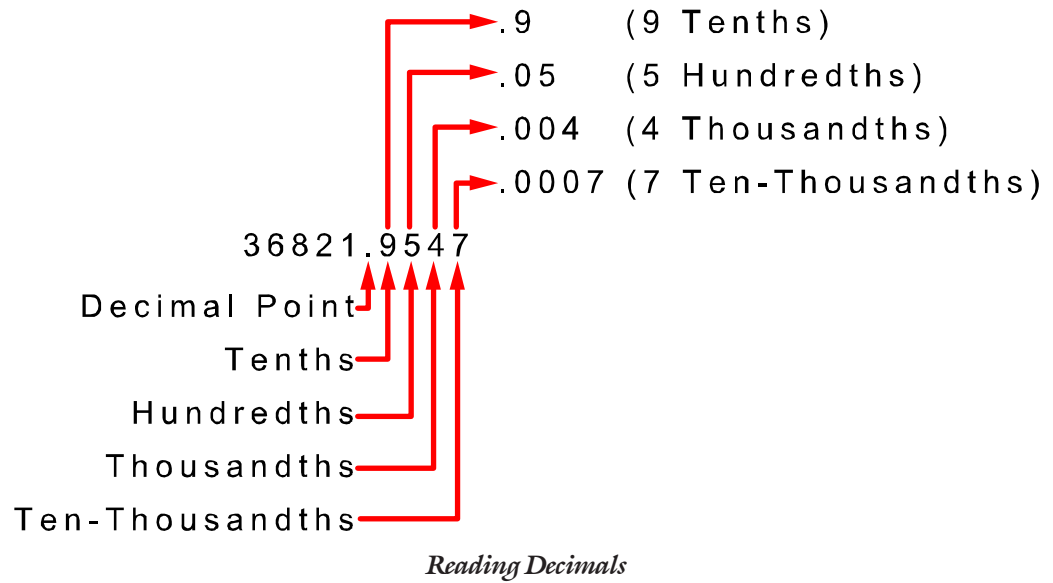
Examples of Decimals

CONTINUE BY SAYING that like whole numbers, each digit of a decimal has a place value.



DISPLAY slide titled “Reading Decimals.”

STATE: “We use the decimal point to separate the whole number from the decimal number.”





Decimals with Zeros

STATE: “We can easily recognize whole numbers with added zeros, but decimals with added zeros can sometimes cause confusion.”

EXPLAIN that the whole number 25 could be written as 025 or 0025. We quickly realize that the zeros are unnecessary. All three numbers (25, 025, and 0025) mean the same. Adding extra zeros to the left of a whole number does not change the number’s value.

CONTINUE BY SAYING that the decimal .25 could be written as .250 or .2500. Like before, the extra zeros are unnecessary. All three decimals (.25, .250, and .2500) mean the same. Adding extra zeros to the right of a decimal does not change the decimal’s value.

EXPLAIN that adding zeros to the right of a whole number does change its value. 25, 250 and 2500 are very different numbers.

CONTINUE BY SAYING that adding zeros between the decimal point and the decimal number changes its value. .25, .025, and .0025 are very different decimals.

STATE: “If there is no whole number, a zero is sometimes added to the left of the decimal point to clarify the decimal.



WRITE “.85 = 0.85” on the flip chart.



Sorting Decimals

STATE: “At first glance, it is often difficult to recognize which decimal is larger or smaller. Some thought and a little practice will help you when comparing decimals.”

EXPLAIN that the easiest method to compare decimals is to give each of the decimals the same number of decimal places by adding zeros to the right.

STATE: “Remember: Adding extra zeros to the right of a decimal does not change the decimal’s value.”

EXPLAIN that initially, .6, .065, .605, and .06 would be difficult to sort.



WRITE .6, .065, .605, and .06 on the flip chart.

CONTINUE BY SAYING that adding zeros to give each decimal the same number of places solves the problem.

EXPLAIN that .600, .065, .605, and .060 are much easier to sort.



WRITE .600, .065, .605, and .060 on the flip chart.

CONTINUE BY SAYING that sorting from the smallest to the largest: .060, .065, .600, and .605



WRITE .060, .065, .600, and .605, in order, on the flip chart.



Adding Decimals

STATE: “Adding decimals is just as easy as adding whole numbers. The key to this process is to align the decimal points.”



WRITE the example on the flip chart.

Examples:

①
$$\begin{array}{r} .457 \\ + .86 \\ \hline \end{array}$$
 Align the decimal points

②
$$\begin{array}{r} .457 \\ + .86 \\ \hline 1.317 \end{array}$$
 Add as with whole numbers

③
$$\begin{array}{r} .457 \\ + .86 \\ \hline 1.317 \end{array}$$
 Bring down the decimal point

EXPLAIN each step of the process.



Subtracting Decimals

STATE: “Aligning the decimal points is also critical when subtracting decimals. It is sometimes helpful to add zeros to the right of one of the numbers to give both numbers the same numbers of decimal places.”

STATE: “Remember: Adding extra zeros to the right of a decimal does not change the decimal’s value.”



WRITE the example on the flip chart.

$$\begin{array}{r} \textcircled{1} \quad 4.3 \\ - 2.859 \\ \hline \end{array}$$

Align the decimal points

$$\begin{array}{r} \textcircled{2} \quad 4.300 \\ - 2.859 \\ \hline \end{array}$$

Insert zeros to give both numbers the same amount of places

$$\begin{array}{r} \textcircled{3} \quad 4.300 \\ - 2.859 \\ \hline 1.441 \end{array}$$

Subtract as with whole numbers

Bring down the decimal point

EXPLAIN each step of the process.



Multiplying Decimals

STATE: “Multiplying decimals is very similar to multiplying whole numbers. With decimals, we must be sure to keep track of the number of decimal places.”



WRITE the example on the flip chart.

Example:

①

$$\begin{array}{r} 5.47 \\ \times .3 \\ \hline \end{array}$$

Align to the right

②

$$\begin{array}{r} 5.47 \\ \times .3 \\ \hline 1641 \end{array}$$

Multiply as with whole numbers

③

$$\begin{array}{r} 5.47 \\ \times .3 \\ \hline 1641 \end{array}$$

2 decimal places
1 decimal places
Count the total number of decimal places (3)

④

$$\begin{array}{r} 5.47 \\ \times .3 \\ \hline 1.641 \end{array}$$

Count the same number of decimal places (3) from the right and insert the decimal point

EXPLAIN each step of the process.



Dividing Decimals

STATE: “Just as with multiplication, the process of dividing decimals is similar to that of whole numbers. As a matter of fact, to make things easier, we will change one of the numbers to a whole number by moving the decimal points on both numbers.”



WRITE the example on the flip chart.

Example:

① $.25 \overline{)40.5}$

② $25 \overline{)40.5}$

Move the decimal all the way to the right

③ $25 \overline{)4050.}$

Move the decimal the same number of places (2)

④ $25 \overline{)4050.}$

Bring the decimal point up

⑤
$$\begin{array}{r} 162. \\ 25 \overline{)4050.} \\ \underline{25} \\ 155 \\ \underline{150} \\ 50 \\ \underline{50} \\ 0 \end{array}$$

Divide as with whole numbers

EXPLAIN each step of the process.



Converting Fractions to Decimals

STATE: “Fractions are often difficult to handle. Sometimes it is easier to change the fraction into a decimal. To change a fraction into a decimal, simply divide the bottom number into the top number.”

STATE: “Example #1: What is the decimal equivalent of $\frac{1}{2}$?”



WRITE the example on the flip chart.

①

$$\frac{1}{2}$$

②

$$2 \overline{)1}$$

Rewrite the problem

③

$$2 \overline{)1.}$$

Add the decimal point

④

$$2 \overline{)1.} \quad \uparrow$$

Bring the decimal point up

⑤

$$\begin{array}{r} .5 \\ 2 \overline{)1.0} \\ \underline{1\ 0} \\ 0 \end{array}$$

Divide as with whole numbers

EXPLAIN each step of the process.



STATE: “Example #2: What is the decimal equivalent of $\frac{3}{16}$?”



WRITE the example on the flip chart.

①

$$\frac{3}{16}$$

②

$$16 \overline{)3}$$

Rewrite the problem

③

$$16 \overline{)3.}$$

Add the decimal point

④

$$16 \overline{)3.0000}$$

Bring the decimal point up

⑤

$$\begin{array}{r} .1875 \\ 16 \overline{)3.0000} \\ \underline{16} \\ 140 \\ \underline{128} \\ 120 \\ \underline{112} \\ 80 \\ \underline{80} \\ 0 \end{array}$$

Divide as with whole numbers

Add as many zeros as is necessary

EXPLAIN each step of the process.



STATE: “Example #3: What is the decimal equivalent of $\frac{25}{100}$?”



WRITE the example on the flip chart.

①

$$\frac{25}{100}$$

②

$$100 \overline{)25}$$

Rewrite the problem

③

$$100 \overline{)25.}$$

Add the decimal point

④

$$100 \overline{)25.} \quad \uparrow$$

Bring the decimal point up

⑤

$$\begin{array}{r} .25 \\ 100 \overline{)25.00} \\ \underline{200} \\ 500 \\ \underline{500} \\ 0 \end{array}$$

Divide as with whole numbers

Add as many zeros as is necessary

EXPLAIN each step of the process.



STATE: “The following is a conversion chart of the most common fractions.

Fraction to Decimal Conversion					
1/32					0.03125
2/32	1/16				0.0625
3/32					0.09375
4/32	2/16	1/8			0.125
5/32					0.15625
6/32	3/16				0.1875
7/32					0.21875
8/32	4/16	2/8	1/4		0.25
9/32					0.28125
10/32	5/16				0.3125
11/32					0.34375
12/32	6/16	3/8			0.375
13/32					0.40625
14/32	7/16				0.4375
15/32					0.46875
16/32	8/16	4/8	2/4	1/2	0.5
17/32					0.53125
18/32	9/16				0.5625
19/32					0.59375
20/32	10/16	5/8			0.625
21/32					0.65625
22/32	11/16				0.6875
23/32					0.71875
24/32	12/16	6/8	3/4		0.75
25/32					0.78125
26/32	13/16				0.8125
27/32					0.84375
28/32	14/16	7/8			0.875
29/32					0.90625
30/32	15/16				0.9375
31/32					0.96875
32/32	16/16	8/8	4/4	2/2	1.0

Conversion Chart

POINT out some common fraction-to-decimal equivalents (e.g. $\frac{1}{2} = .5$, $\frac{1}{4} = .25$, $\frac{1}{8} = .125$, etc.)



Progress Check #3



DIRECT the participants to the section titled “Progress Check # 3” in their Participant Guide.

ALLOW them enough time to complete the Progress Check and then review the answers.

1. Put the following decimals in order from smallest to largest:

a. .031, .31, .301, and .0031

.0031, .031, .301, .31

b. 0.2, .207, .027, and .27

.027, 0.2, .207, .27

2. Add the following decimals:

a. $.45 + .528 + .3 = \underline{1.278}$

b. $.8 + .37 + 1.366 = \underline{2.536}$

3. Subtract the following decimals:

a. $.56 - .379 = \underline{.181}$

b. $1.3 - .299 = \underline{1.001}$

4. Multiply the following decimals:

a. $2.54 \times 5.3 = \underline{13.462}$

b. $.741 \times .44 = \underline{.32604}$



5. Divide the following decimals:

a. $4.24 \div 1.06 = \underline{4}$

b. $20.215 \div .05 = \underline{404.3}$

6. Convert the following fractions to decimals:

a. $\frac{1}{4} = \underline{.25}$

b. $\frac{3}{8} = \underline{.375}$

7. Your company pays independent truckers 32 cents for each mile traveled. The truckers each traveled different distances (see below). What is the total amount of money your company will pay these truckers?

Trucker A: 354.6 miles

Trucker B: 753.9 miles

Trucker C: 1,321.4 miles

Trucker D: 448.1 miles

\$920.96

8. You worked 46 hours this week. Anything over 40 hours is paid at time-and-a-half ($1.5 \times$ pay). Your regular hourly pay is 11.50 per hour. What was your gross income (before taxes) this week?

\$563.50



Percents



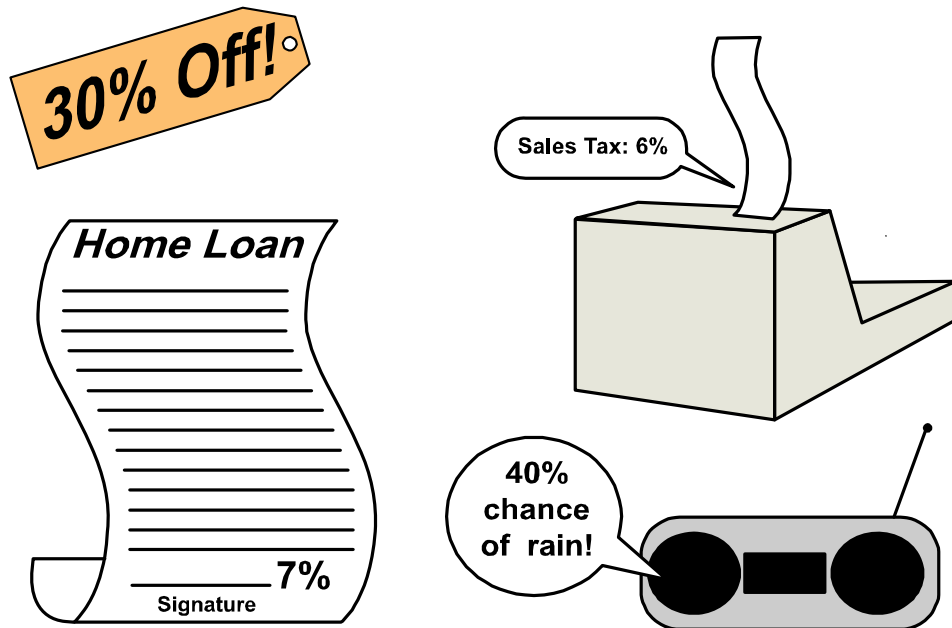
DIRECT the participants to the section titled “Percents” in their Participant Guides.



DISPLAY the slide titled “Examples of Percents.”

STATE: “Just as fractions and decimals are everywhere, so are percents. Percents are another way of describing part of a whole. In the case of percents, the whole is divided into 100 equal parts.”

EXPLAIN that a store that advertises “30% off!” is telling us that prices will be reduced 30 cents for every dollar, and a loan that offers 7% interest charges \$7 for every \$100 borrowed.



Examples of Percents



Converting Percents to Fractions and Decimals

STATE: “Since percents are based on 100 parts, changing percents to fractions involves placing the percent over 100.”

EXPLAIN that dividing the top number by 100 converts the fraction to a decimal.



WRITE the examples on the flip chart.

$$50\% = \frac{50}{100} = .50$$

$$75\% = \frac{75}{100} = .75$$

$$100\% = \frac{100}{100} = 1.00$$

$$140\% = \frac{140}{100} = 1.40$$

EXPLAIN each step of the process.

STATE: “100% is equal to the whole, 200% is two times the whole, etc.”



Converting Fractions and Decimals to Percents

STATE: “Previously, we saw how to convert a fraction to a decimal. We simply divided the top number by the bottom number. We will use this same method to convert a fraction to a percent. Then we will convert the decimal to a percent by multiplying it by 100. (After all, percents are based on 100.)”



WRITE the examples on the flip chart.

$$\frac{1}{4} = .25 \times 100 = 25\%$$

$$\frac{3}{8} = .375 \times 100 = 37.50\%$$

$$\frac{2}{3} \approx 0.667 \times 100 = 66.7\%$$

$$\frac{7}{16} = 0.4375 \times 100 = 43.75\%$$

$$\frac{1}{20} = 0.05 \times 100 = 5\%$$

EXPLAIN each step of the process.



Working with Percents

STATE: “Solving problems with percents is a matter of multiplication or division.”



WRITE the examples on the flip chart.

Examples:

- a. 30% of \$175 is ?
 .30 of \$175 is ? Convert the percent to a decimal
 .30 X \$175 = \$52.50 Multiply
- b. 45% of \$342 is ?
 0.45 of \$342 is ? Convert the percent to a decimal
 0.45 X \$342 = \$153.90 Multiply
- c. What percent of 34 is 17?
 ?% of 34 is 17 Write the problem
 ?% = $\frac{17}{34}$ Rewrite the problem
 ?% = .50 Convert fraction to a decimal
 ?% = 0.5 X 100 Convert decimal to percent
 ?% = 50%
- d. What percent of 500 is 25?
 ?% of 500 is 25 Write the problem
 ?% = $\frac{25}{500}$ Rewrite the problem
 ?% = .05 Convert fraction to a decimal
 ?% = .05 X 100 Convert decimal to percent
 ?% = 5%

EXPLAIN each step of the process.



Progress Check #4



DIRECT the participants to the section titled “Progress Check # 4” in their Participant Guide.

ALLOW them enough time to complete the Progress Check and then review the answers.

1. Convert the following percents to fractions (reduce as necessary):

- a. 35% $\frac{7}{20}$
- b. 6% $\frac{3}{50}$
- c. 21.9% $\frac{219}{1000}$

2. Convert the following percents to decimals:

- a. 68% $.68$
- b. 3.3% $.033$
- c. 119% 1.19

3. Convert the following fractions to percents:

- a. $\frac{3}{4}$ 75%
- b. $\frac{2}{5}$ 40%
- c. $\frac{21}{50}$ 42%

4. Convert the following decimals to percents:

- a. .89 89%
- b. .08 8%
- c. .576 57.6%



5. Seven and one-half percent of your pay is taken for Social Security. If your gross pay is \$386, how much money do you contribute to your social security account?

\$28.95

6. Your lift truck operators loaded 159 pallets onto trucks. Fifty-three of the pallets contained birdseed. What percent of the pallets had birdseed?

33.33%



Measurements



DIRECT the participants to the section titled “Measurements” in their Participant Guides.

STATE: “There are many times when we must ensure that the product we are storing or shipping meets space requirements. Measurements are often taken to ensure the product will fit into a carton, on a rack or onto a trailer. As a warehouse team member, you may be responsible for taking these measurements.”

EXPLAIN that there are two measurement systems in use throughout the United States and the world – the standard, or “American” measuring system and the metric system.

EXPLAIN that we will cover both.

Linear Measurements

STATE: “Because warehouse personnel are not required to measure much more than a few feet, we will only focus on three units of measuring distance in each system: The inch, the foot and the yard in the standard system, and the millimeter, centimeter and meter in the metric system.”

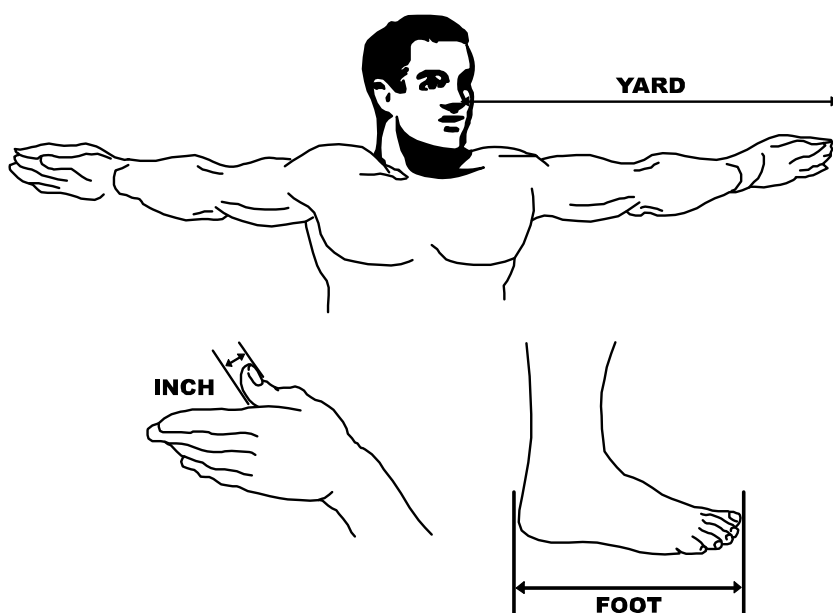
Standard System



DISPLAY slide titled “Standards.”

STATE: “The standard system has unusual origins. Centuries ago, the units of measurements were based on rather dubious “standards.” An inch was the width of a thumb. A foot was the length of a foot from the heel to the tip of the big toe. A yard was the distance from the tip of the nose to the tip of the middle finger.”

EXPLAIN that it is easy to see that there are great inconsistencies between one person’s thumb and another’s. There are even greater differences between the size of our feet! And which way should we turn our head (and nose) when measuring a yard?



Standards



CONTINUE BY SAYING that these “standards” may have been sufficient three hundred years ago, but they certainly are not adequate in the 21st century.

EXPLAIN that the standard system has evolved from those primitive measurements to scientifically accurate standards. An inch has been standardized as equal to the wavelength of light given off by Krypton 86 gas. It is an absolute standard that never changes.

STATE: “The abbreviation for an inch is **in.**”



WRITE “in” on the flip chart.

STATE: “One inch is often written as **1”.**”



WRITE 1" on the flip chart.

EXPLAIN that a foot is twelve times an inch. That is, there are twelve inches in a foot.

STATE: “1 foot = 12 inches.”

STATE: “The abbreviation for a foot is **ft.**””

STATE: “One foot is often written as **1’.**”

EXPLAIN that a yard is three times a foot. That is, there are three feet in a yard.

STATE: “1 yard = 3 feet”

STATE: “The abbreviation for a yard is **yd.**””



WRITE “yd” on the flip chart.



EXPLAIN that since there are twelve inches in a foot, there must be 36 inches in a yard. ($3 \times 12" = 36"$)



WRITE the following chart on the flip chart.

12 inches = 1 foot

3 feet = 1 yard

36 inches = 1 yard

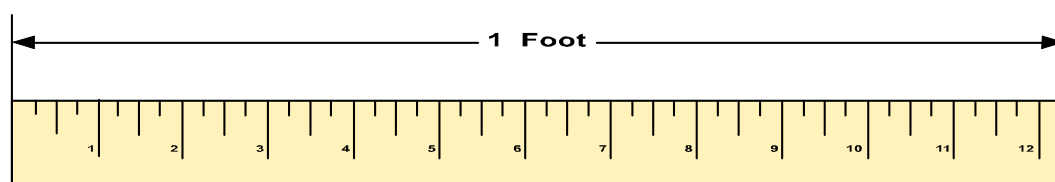
Rulers, Yardsticks and Tape Measures

STATE: “When measuring small distances we commonly use rulers, yardsticks or tape measures.”



DISPLAY the slide titled “Ruler.”

STATE: “A ruler, sometimes referred to as a “foot rule” or “straightedge,” is one foot long. It is useful when measuring distances less than twelve inches.”

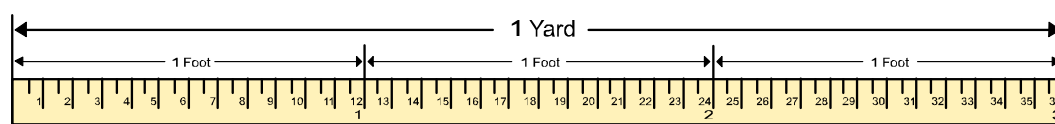


Ruler



DISPLAY the slide titled “Yardstick.”

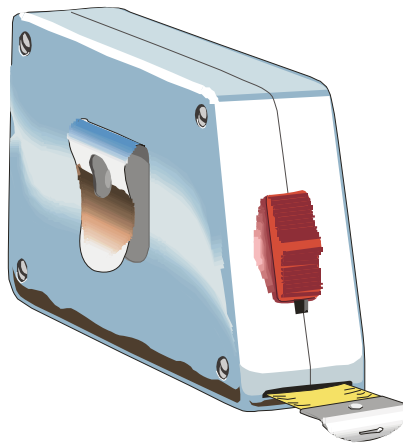
STATE: “A yardstick is one yard long. It is three times the length of a ruler. It is useful when measuring distances less than 36 inches.”



Yardstick



EXPLAIN that tape measures come in a variety of sizes (16', 20', etc.). Because a tape measure is retractable and flexible, it may be extended a small amount or its entire length. A tape measure is useful when measuring distances from a few inches to several feet. It is convenient to carry or store.



Tape Measure

CONTINUE BY SAYING that rulers, yardsticks and tape measures are marked at each inch. Yardsticks and tape measures also have markings at each foot.

STATE: “A ruler is divided into twelve inches.”

STATE: “A yardstick is divided into 36 inches.”

EXPLAIN that although tape measures come in different sizes, they are also divided into inches and feet along their entire length.



Smaller Measurements

STATE: “In today’s era of mass production, a foot and an inch are rather large measurements. Therefore, the inch has been divided into smaller parts.”

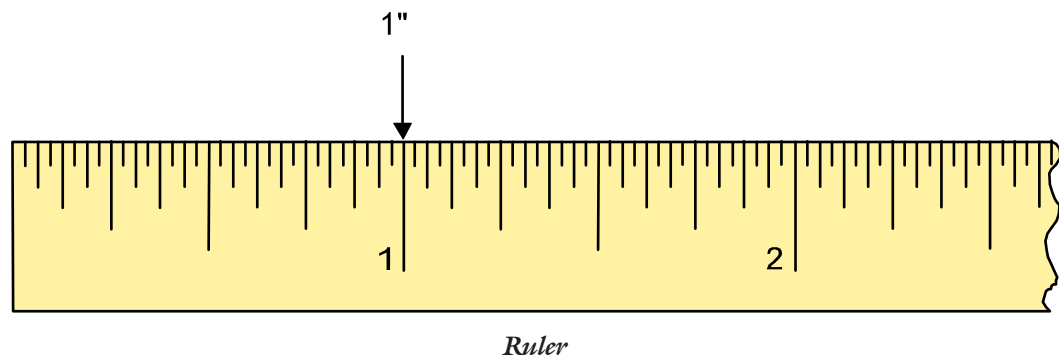
Graduations

EXPLAIN that on each of these measuring tools, there are several difference-sized markings. The longest of these “graduations” marks a full inch. The first inch mark is one inch from the left end of the ruler.



DISPLAY slide titled “Ruler.”

POINT to the one-inch mark.



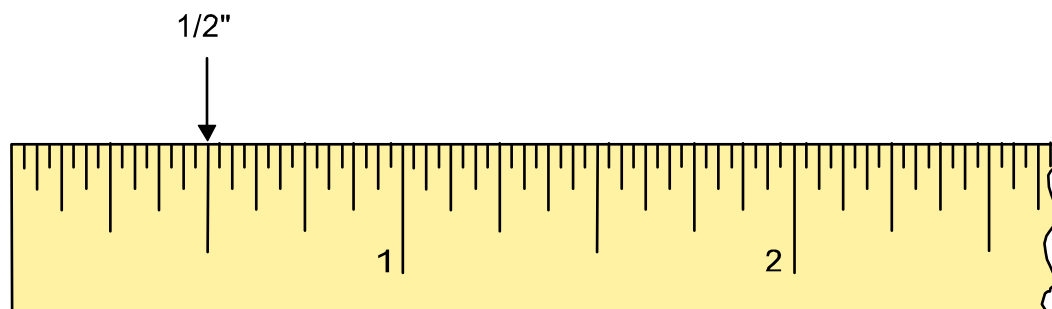
STATE: “There is a mark for every inch along the ruler, yardstick or tape measure. The marks are numbered in sequence (i.e. 1, 2, 3, 4, etc.).”

EXPLAIN that when linear measurements are taken, they often fall between the inch markings. If we look more closely at a ruler, yardstick or tape measure, we can see that there are many graduations of different sizes between each inch mark.

CONTINUE BY SAYING that these markings help us divide an inch into parts or fractions.

EXPLAIN that the second longest graduation marks the halfway point between each inch. It represents one-half inch. The first half-inch mark is one-half of an inch from the left end of the ruler.

POINT to the one-half inch mark.



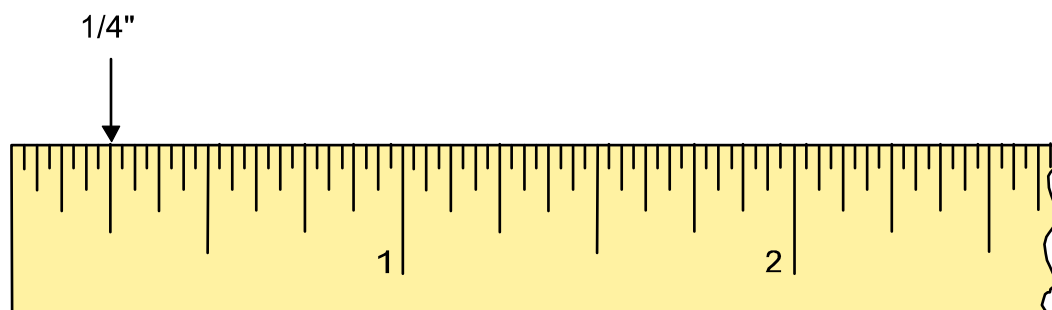
STATE: “One-half inch is written as a fraction: $\frac{1}{2}$ ”.



WRITE $\frac{1}{2}$ ” on the flip chart.

EXPLAIN that the next longest graduation marks each one-fourth inch. The first quarter-inch mark is one-fourth of an inch from the left end of the ruler.

POINT to the one-fourth inch mark.



STATE: “One-fourth inch is written as a fraction: $\frac{1}{4}$ ”.

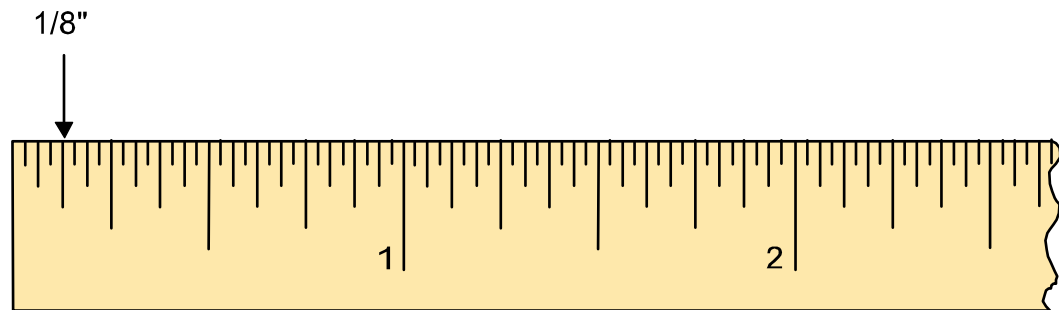


WRITE $\frac{1}{4}$ ” on the flip chart.



EXPLAIN that the next longest graduation marks each one-eighth inch. The first eighth-inch mark is one-eighth of an inch from the left end of the ruler.

POINT to the one-eighth inch mark.



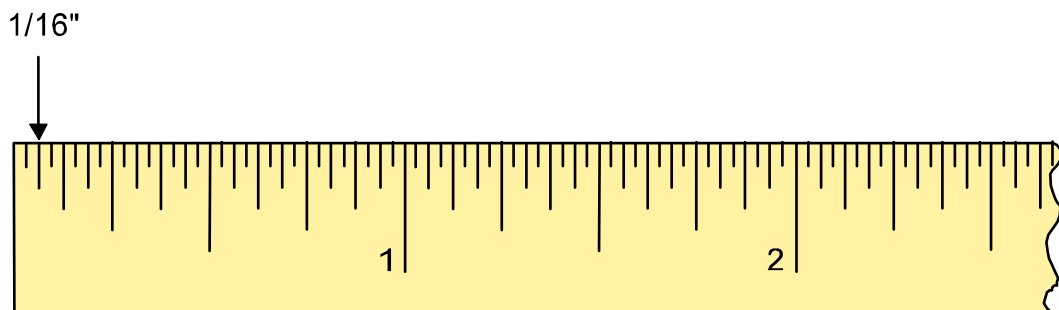
STATE: “One-eighth inch is written as a fraction: $\frac{1}{8}$ ”.



WRITE $\frac{1}{8}$ " on the flip chart.”

EXPLAIN that the next longest graduation marks each one-sixteenth inch. The first sixteenth-inch mark is one-sixteenth of an inch from the left end of the ruler.

POINT to the one-sixteenth inch mark.



STATE: “One-sixteenth inch is written as a fraction: $\frac{1}{16}$ ”.

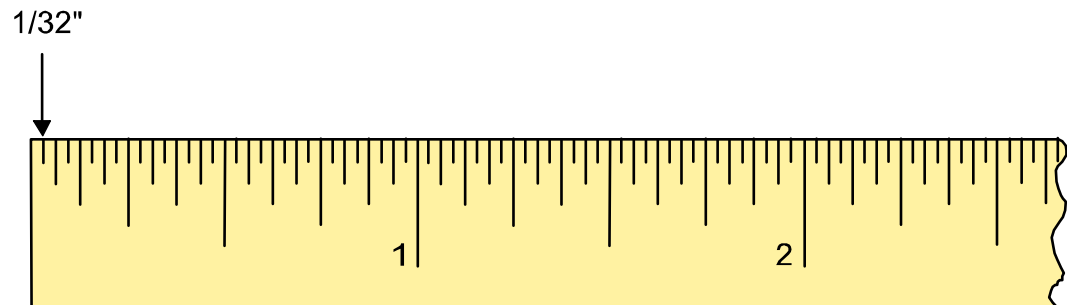


WRITE $\frac{1}{16}$ " on the flip chart.



EXPLAIN that the next longest graduation represents each one thirty-seconds inch. The first thirty-seconds of an inch mark is one thirty-seconds of an inch from the left end of the ruler.

POINT to the one thirty-seconds inch mark.



STATE: “One thirty-seconds inch is written as a fraction: $\frac{1}{32}$ ”.



WRITE $\frac{1}{32}$ on the flip chart.

EXPLAIN that only precision rulers go much smaller than $\frac{1}{32}$.

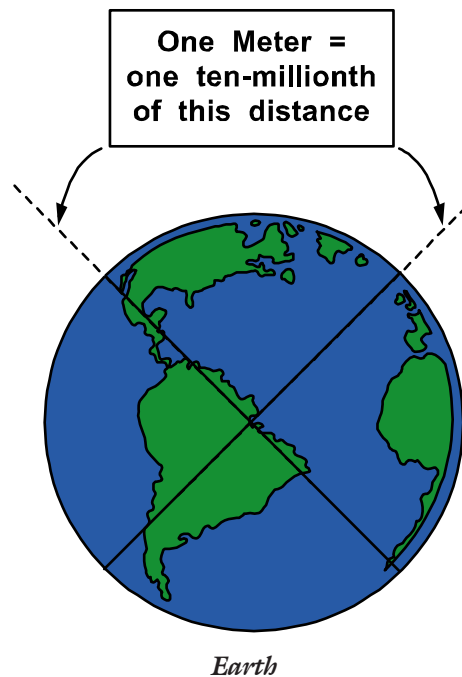
CONTINUE BY SAYING that if a measurement exceeds an inch, we simply look at the whole-inch to the immediate left and then add the fraction.

Metric System



DISPLAY the slide titled “Earth.”

STATE: “The metric system has a much more scientific origin. In 1790, at the request of the French Parliament, the French Academy of Sciences proposed a measuring system based on one unit of measurement...the meter. A meter was determined to be one-ten millionth of the distance from the North Pole to the equator.”



EXPLAIN that the French adopted the metric system in 1795, but the rest of the world was slow to follow. In 1875, the Treaty of the Meter, establishing the meter as an international standard, was signed by 17 nations, including the United States. One hundred years after that, in 1975, the U.S. Congress passed a law which encouraged the voluntary conversion to the metric system. A quarter of a century later, the United States has made some progress towards adopting the meter as its universal standard.

EXPLAIN that the meter is used as the basis for most other measurements in the metric system (liquid measures, weight, etc.)

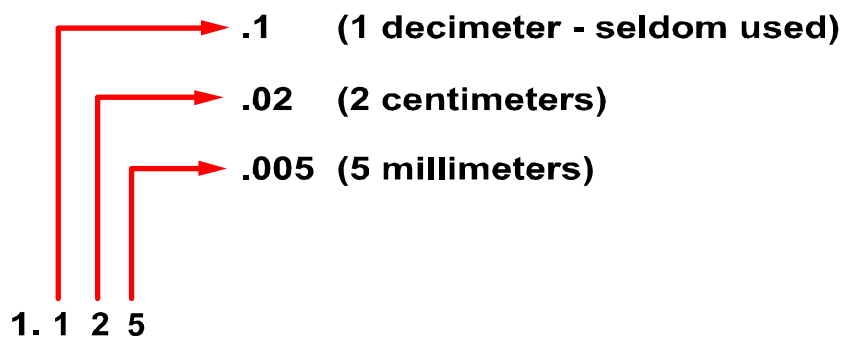


STATE: “The abbreviation for a meter is **“m.”**”



WRITE “m” on the flip chart.

DISPLAY the slide titled “Metric Place Values.”



Metric Place Values

STATE: “A meter contains 100 centimeters.

(Note: “centi” means hundredths.)”

STATE: “The abbreviation for a centimeter is **“cm.”**”



WRITE “cm” on the flip chart.

EXPLAIN that a meter also contains 1000 millimeters.

(Note: “milli” means thousandths.)

STATE: “The abbreviation for a millimeter is **“mm.”**”



WRITE “mm” on the flip chart.

EXPLAIN that since there are 1000 millimeters in a meter and 100 centimeters in a meter, there must be 10 millimeters in a centimeter ($1000 \div 100 = 10$).



WRITE the following chart on the flip chart.

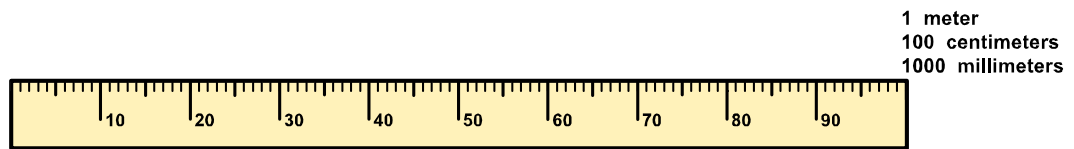
1 meter	=	100 centimeters
1 meter	=	1000 millimeters
1 centimeter	=	10 millimeters
1 centimeter	=	.01 meter
1 millimeter	=	.001 meter

Meter Measuring Stick



DISPLAY the slide titled “Meter Stick.”

STATE: “A meter measuring stick is one meter long. It has 1000 marks indicating each millimeter. There are larger graduation marks for each centimeter as well as every five and ten centimeters.”



Meter Stick



Progress Check # 5



DIRECT the participants to the section titled “Progress Check # 5” in their Participant Guide.

ALLOW them enough time to complete the Progress Check and then review the answers.

1. Using a standard ruler, measure the lines below:

a.

b.

c.

2. Using a metric ruler, measure the same lines.
3. Using a yardstick or tape measure, measure the length, width and height of your desk.
4. Using a meter measuring stick or tape measure, measure the length, width and height of your desk.

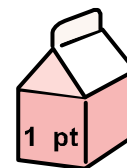
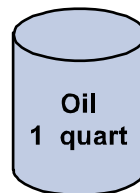
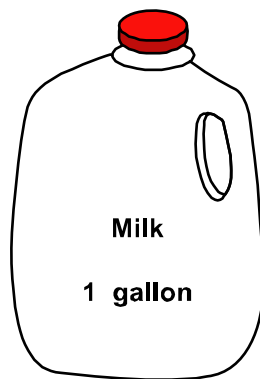
Liquid Measures

Standard System

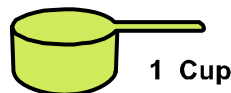


DISPLAY the slide titled “Examples of Liquid Standards.”

STATE: “Measuring liquid volume (or capacity) using the standard system is quite awkward. Of uncertain origin, the gallon (from “galleon” or vessel) is the basic measure of liquid volume. A gallon is divided into four quarts (or “quarters”). The quart contains two pints (possibly from the “paint” mark dividing a quart container in half). A pint has two cups and a cup has 8 ounces.”



Whipping Cream

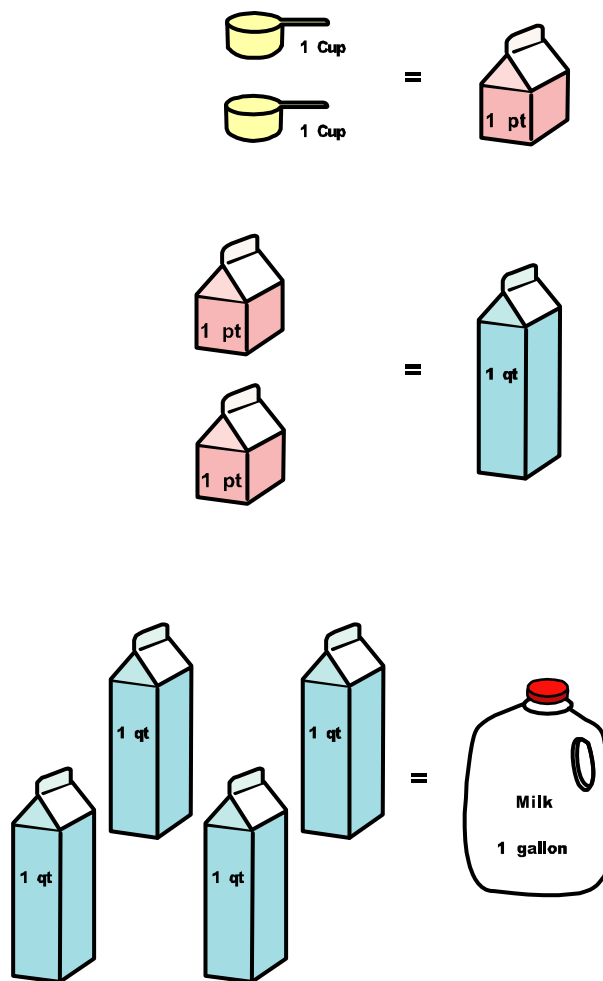


Examples Liquid Standards



DISPLAY the slide titled “Equivalents of Liquid Standards.”

EXPLAIN that the standard system is not very scientific, but we are stuck with it.



Equivalents of Liquid Standards

STATE: “The abbreviation for gallon is gal.”



WRITE “gal” on the flip chart.

STATE: “The abbreviation for quart is qt.”



WRITE “qt” on the flip chart.



STATE: “The abbreviation for pint is **pt.**”



WRITE “pt” on the flip chart.

STATE: “The abbreviation for ounce is **oz.**”



WRITE “oz” on the flip chart.

EXPLAIN that there is no standard abbreviation for cup.



WRITE the following chart on the flip chart.

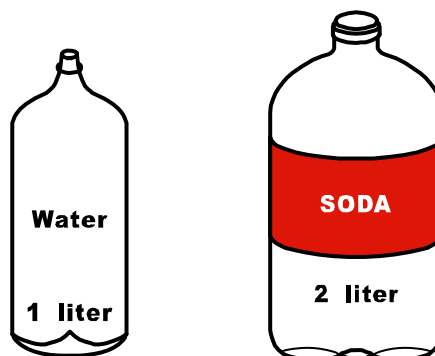
			1 cup	= 8 ounces
		1 pint	= 2 cups	= 16 ounces
	1 quart	= 2 pints	= 4 cups	= 32 ounces
1 gallon	= 4 quarts	= 8 pints	= 16 cups	= 128 ounces

Metric System



DISPLAY the slide titled “Examples of Liquid Metrics.”

STATE: “On the other hand, measuring liquid volume using the metric system is quite simple. Based on the meter, the basic unit of liquid measurement is the liter. A liter is equal to 1,000 cubic centimeters.”



Examples of Liquid Metrics



DISPLAY the slide titled “Equivalents of Liquid Metrics.”

EXPLAIN that a milliliter is one-thousandth of a liter. Therefore, a cubic centimeter is equal to a milliliter.



One Cubic Centimeter



$$\times 1000 =$$



Equivalent of Liquid Metrics



WRITE the following chart on the flip chart.

$$1 \text{ liter} = 1000 \text{ cu cm}$$

$$1 \text{ liter} = 1000 \text{ milliliters}$$

$$1 \text{ cu cm} = 1 \text{ milliliter}$$

Weights

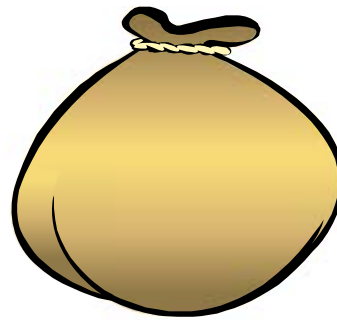
Standard System

STATE: “The basic unit of weight in the standard system is the pound (from the Latin “pundus” meaning “weight”). There are sixteen ounces in a pound.”

STATE: “The abbreviation for pound is “**lb**” (from the Latin “libra” meaning scales).”



1 lb of cheese



5 lb of potatoes



WRITE “lb” on the flip chart.

STATE: “There are two thousand pounds in a ton.”

STATE that the abbreviation for ton is “**T**.”



WRITE “T” on the flip chart.

WRITE the following chart on the flip chart.

1 pound = 16 ounces

1 ton = 2000 pounds



Metric System

STATE: “Also based on the meter, the basic unit of weight in the metric system is the gram. A gram is equal to the weight of one cubic centimeter of water.”

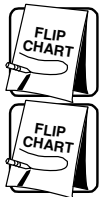
EXPLAIN that a kilogram is one thousand grams. One kilogram (or “kilo”) is equal to the weight of a liter (1,000 cubic centimeters) of water.

STATE that the abbreviation for grams is “g.”



WRITE “g” on the flip chart.

STATE that the abbreviation for kilogram is “kg.”



WRITE “g” on the flip chart.

WRITE the following chart on the flip chart.

1 gram = 1 cu cm of water

1 kilogram = 1000 grams



Progress Check # 6



DIRECT the participants to the section titled “Progress Check # 6” in their Participant Guide.

ALLOW them enough time to complete the Progress Check and then review the answers.

1. One of our buyers made a purchase of five 55-gallon drums of hummingbird nectar. In order to save money, the purchasing manager has asked the warehouse personnel to fill the nectar containers for sale. Assuming no spillage, how many pint-sized containers can we fill?

2200 pint-sized containers

2. The warehouse has mistakenly received 52,000 bags of grass seed instead of birdseed. Each bag weighs 4 ounces. The transportation manager needs to know how many tons of birdseed he must ship back to the vendor. How many tons are there?

6.5 tons

3. Because of the previous error and in order to meet customer demands, the warehouse manager has decided to use the 400 kg of bulk birdseed that is stored in the warehouse. How many bags of birdseed will we be able to fill (assuming no losses) if each bag contains 250 g of birdseed?

1600 bags



Graphs



DIRECT the participants to the section titled “Graphs” in their Participant Guide.

STATE: “Graphs provide a visual representation of numbers. They allow us to quickly see changes, compare numbers to each other, or compare part of something to the whole thing.”

EXPLAIN that graphs help to simplify complicated sets of numbers.

CONTINUE BY SAYING that managers often use graphs to better understand what is happening to the company (productivity, efficiency, costs, etc.). Employees often receive graphs of their investments in their retirement accounts. The news media sometimes uses graphs to show how much money our government is spending.

STATE: “There are three basic types of graphs: Pie, Bar and Line.”



Pie Graph

STATE that pie graphs (or circle graphs) allow us to compare parts of a whole. The circle represents the whole thing...100% of whatever “it” might be: the number of employees, the total budget, all of the inventory, etc.

EXPLAIN that the slices of the pie graph represent parts (percentages) of the whole...the number of managers, the money spent on lift truck repair, the quantity of inventory requiring refrigeration.

CONTINUE BY SAYING that to develop a pie chart, determine the overall total. Then calculate what percentage of the total each part is.

STATE: “Example #1: The warehouse operates three shifts. The chart below indicates how many employees are on each shift.”

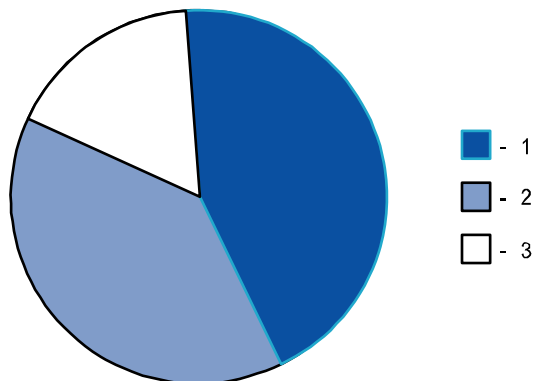


DISPLAY the slide titled “Pie Graph.”

EXPLAIN that from this pie graph we can easily see that the first shift has more employees than second or third shift, but second and third shift combined have more employees than first.

Shift	#of Employees	%
1st	224	47.6%
2nd	182	38.6%
3rd	65	13.8%
Total	471	100%

Employees by Shift



Pie Graph



Bar Charts

STATE: “To compare one number against others, bar charts are used. Bar graphs are sometimes called column graphs. No calculations are required since the raw numbers are used.”

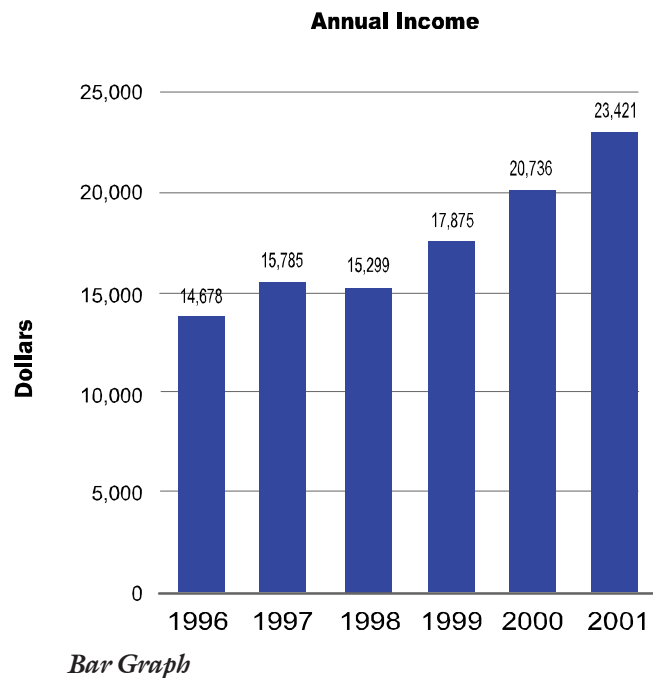
STATE: “Example #2: Annual income over a six-year period.”



DISPLAY the slide titled “Bar Graph.”

EXPLAIN that from the above graph, we can see that 1998 was this person’s smallest annual income, while 2001 was the largest.

Year	Income
1996	14,678
1997	15,785
1998	15,299
1998	17,875
2000	20,736
2001	23,421





Line Graphs

STATE: “When we are interested in changes or trends, we can use a line graph. Again, no calculations are necessary since the raw numbers are used.”

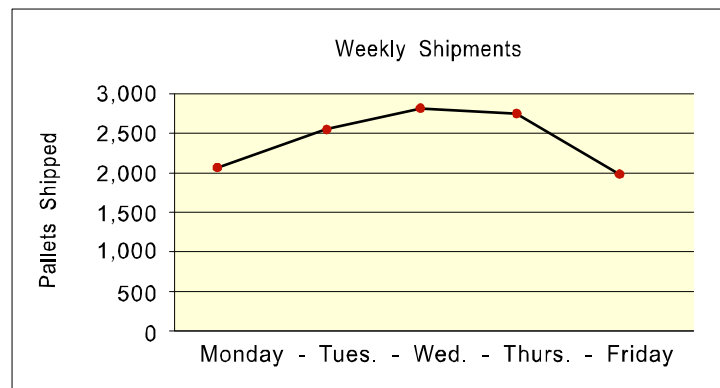
STATE: “Example #3: Daily Production.”



DISPLAY the slide titled “Line Graph.”

EXPLAIN that in this line graph we can see that more work gets done during the middle of the week.

Monday	2,163
Tuesday	2,598
Wednesday	2,743
Thursday	2,682
Friday	1,955



Line Graph

ASK: “Why do you think production lags on Monday and Friday?”



Averages

STATE that an average is something that is in the middle of a group or represents what is most common in the group. In statistics, the average is referred to as the “mean.”

EXPLAIN that averages are important because they give us a quick “snapshot” of a group of numbers.

CONTINUE BY SAYING that knowing the average amount of product fabricated each day enables a manager to determine how many units can be fabricated during an average week or month.

CONTINUE BY SAYING that knowing the average number of defects on a machine each day enables the Quality Department to monitor trends and take action when the number of defects begins to deviate from the norm, that is, the average.



Calculating an Average

STATE: “Determining an average requires two of the basic skills we have already discussed: adding and dividing.”

EXPLAIN that we must first add all of the numbers in the group being averaged. Then we must divide the total by the number of items in the group.

STATE: “Example 1: Your child received the following school grades:”



WRITE the following grades on the flip chart.

English	85
U.S. History	77
Mathematics	92
Science	84
Physical Education	72

EXPLAIN that, to determine how well your child is doing in school, you must determine the average grade.

EXPLAIN that, using the addition process, we must add all five grades together. Then, using the division process, we must divide the total (410) by the number of grades in the group (5).

CONTINUE BY SAYING that, completing the process, you learn that your child’s average grade is 82.



Progress Check #7



DIRECT the participants to the section titled “Progress Check # 7” in their Participant Guide.

ALLOW them enough time to complete the Progress Check and then review the answers.

1. Match the type of chart to its most common use.

C Pie A. To compare one number against another.

A Bar B. To show trends.

B Line C. To compare parts of a whole.

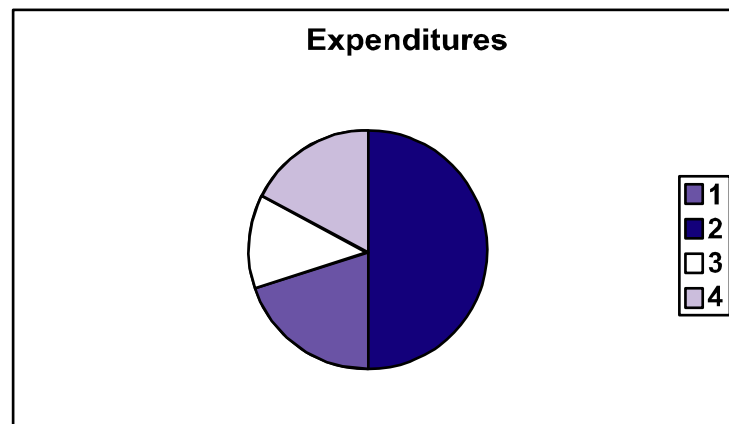
2. Create a pie graph showing the amount of money spent on each category.

Building Lease: \$420,000

Utilities: \$174,000

Maintenance: \$112,000

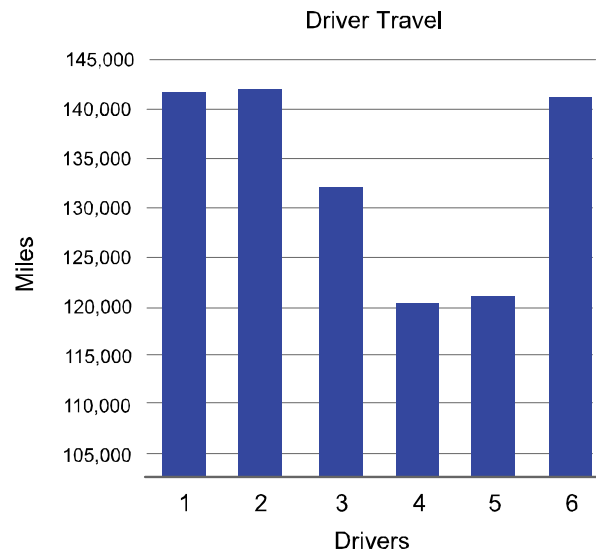
Taxes: \$134,000





3. Using the bar graph below, which driver traveled the most miles?
The fewest?

1. Bill	142,467
2. Bob	142,877
3. Mary	132,765
4. Mark	120,875
5. Karla	121,554
6. Wayne	141,235

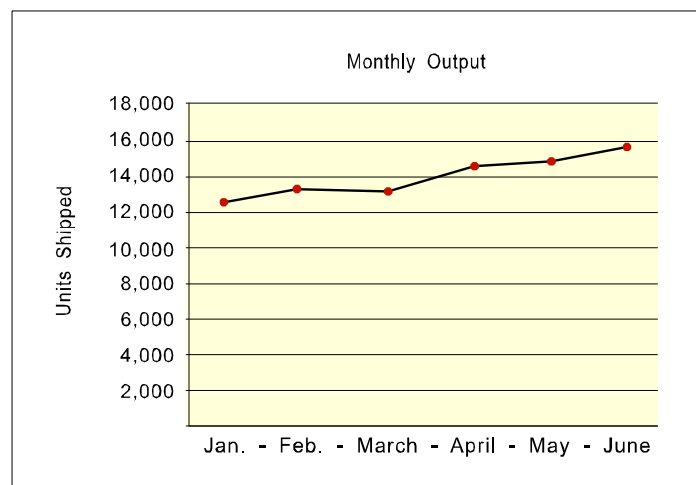


Most: Driver # 2.

Fewest: Driver # 4.

4. Using the line chart below, predict the approximate number of units that will be shipped in July.

January	12,286
February	13,352
March	13,289
April	14,322
May	14,688
June	15,786



- a. Approximately 12,000 c. Approximately 16,000
b. Approximately 14,000 d. Approximately 18,000

5. Calculate the average height of all of the participants in your class.



Geometry

Angles



DIRECT the participants to the section titled “Geometry” in their Participant Guides.

STATE: “An angle is formed when two straight lines meet.”

EXPLAIN that the size of the angle is the amount of turn that is needed to take one line and place it on top of the other line.

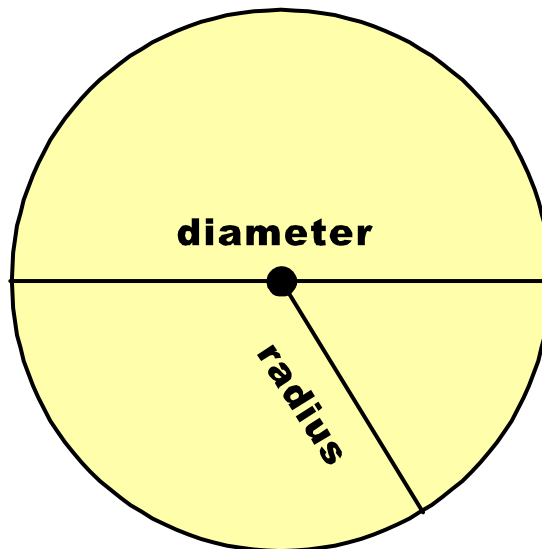
STATE: “The amount of turn is measured in degrees.”

STATE: “Degrees are indicated by a small “°” above the number.”

STATE: “There are 360° in a full circle.”



DRAW a circle on the flip chart.

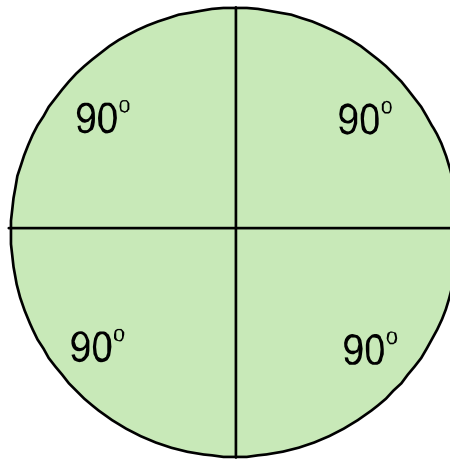


Right Angles

EXPLAIN that, if we cut a circle into four equal parts, each of the angles that are formed would contain 90° .



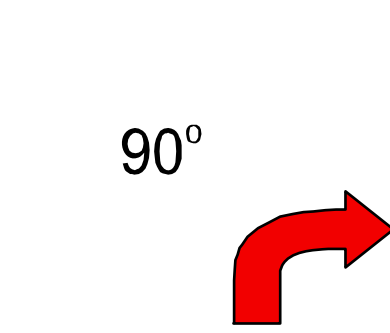
DRAW on the flip chart lines to separate the circle into four equal parts.



CONTINUE BY SAYING that, looking at just one of those parts, we can see that a 90° angle would equal a quarter of a complete turn through the circle.

STATE: “Squares and rectangles contain four 90° angles.”

STATE: “A 90° angle is commonly referred to as a right angle.”





Acute Angles

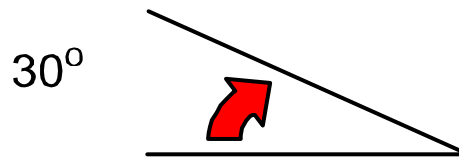
STATE: “Acute angles are angles that are less than 90° .”

STATE: “Common acute angles are 30° , 45° , and 60° .”

STATE: “ 30° is one-third of a 90° angle.”



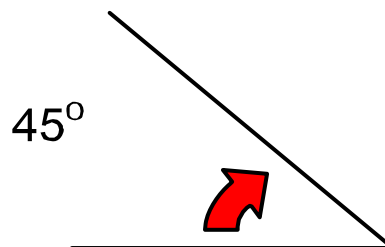
DRAW a 30° angle on the flip chart.



STATE: “ 45° is half of a 90° angle.”



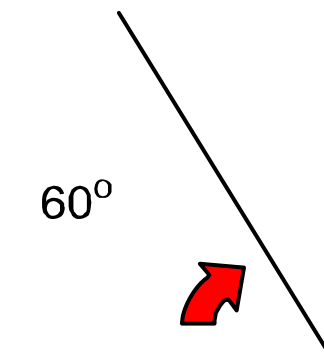
DRAW a 45° angle on the flip chart.



STATE: “ 60° is two-thirds of a 90° angle.”



DRAW a 60° angle on the flip chart.



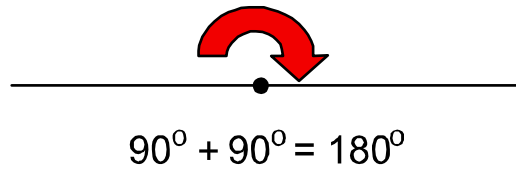


Straight Angles

STATE: “If we cut a circle into two equal parts, each of the angles that are formed would contain 180° .”



DRAW on the flip chart a line through a circle.



EXPLAIN that looking at just one of those parts, we can see that a 180° angle would equal half of a complete turn through the circle.

STATE: “A 180° angle is commonly referred to as a straight angle.”



Obtuse Angles

STATE: “Obtuse angles are angles that are greater than 90° .”

EXPLAIN that, as stated previously, if we cut a circle into four equal parts, each of the angles that are formed would contain 90° .



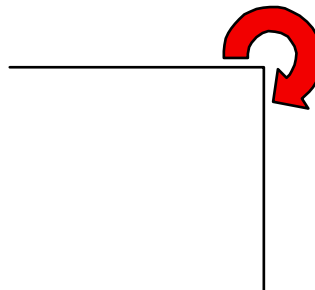
DRAW on the flip chart a circle with four equal parts.

EXPLAIN that, looking at three of those parts, we can see that a 270° angle ($3 \times 90^\circ$) would equal a three-quarter turn through the circle.

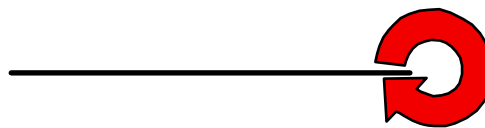


DRAW a 270° angle on the flip chart.

$$90^\circ + 90^\circ + 90^\circ$$



EXPLAIN that, looking at all four of those parts, we can see that a 360° angle ($4 \times 90^\circ$) would equal a complete turn through the circle.



$$90^\circ + 90^\circ + 90^\circ + 90^\circ = 360^\circ$$

Common Shapes

STATE: “There are several common shapes that we all recognize. Understanding their makeup and how to measure them is important.”



DISPLAY the slide titled “Common Shapes.”

Square

STATE: “All four sides of a square are equal. All four angles are 90° . The total of all four angles is 360° . The opposite sides are parallel to each other.”



Squares

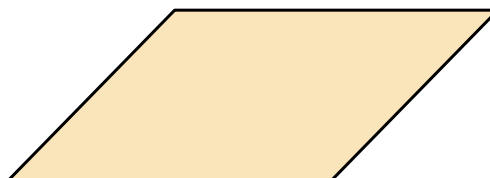
Rectangle

STATE: “Opposite sides are equal. All four angles are 90° . The total of all four angles is 360° . The opposite sides are parallel to each other.”



Parallelogram

STATE: “Opposite sides are equal. Opposite angles are equal. The total of all four angles is 360° . The opposite sides are parallel to each other.”





Triangles

STATE: “A triangle has three sides. The total of all three angles is 180° . There are many different kinds of triangles.”



DISPLAY the slide titled “Triangles.”

Equilateral Triangle

STATE: “All three sides are equal. All three angles are 60° .”

Isosceles Triangle

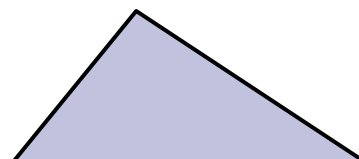
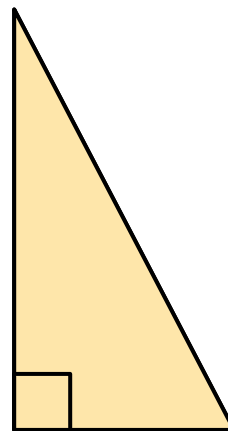
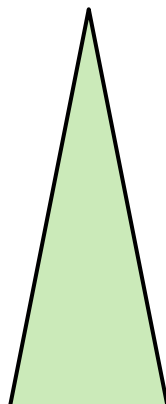
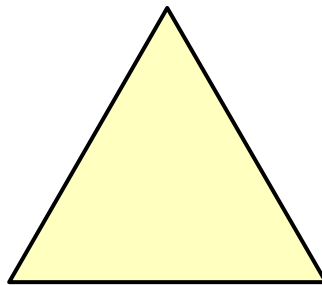
STATE: “Two sides are equal. Two angles of the triangle are equal.”

Right Triangle

STATE: “One angle of the triangle is 90° .”

Scalene Triangle

STATE: “No equal sides. No equal angles. No angle is 90° .”



Triangles

Circles



DISPLAY the slide “Circle”

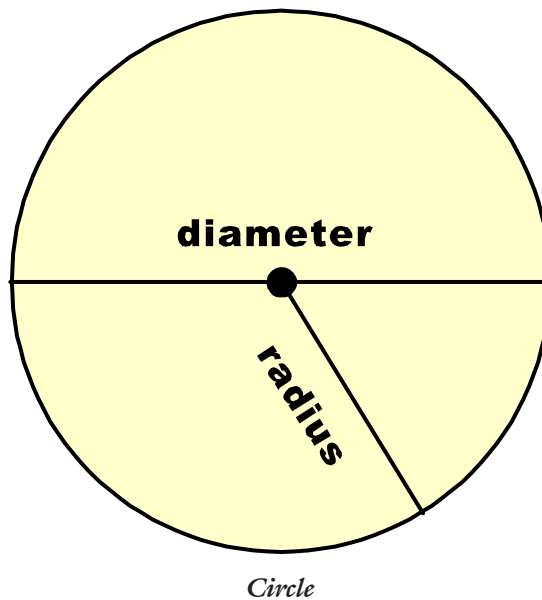
STATE: “A circle is perfectly round. That is to say that all points on the circle are an equal distance from its center.”

Radius

STATE: “A line drawn from the center of the circle to its edge is called a radius.”

Diameter

STATE: “A line drawn from one edge through the center to another edge is called a diameter. A diameter is equal to two radii.”





Measuring Shapes

Perimeter

STATE: “The distance around a two-dimensional (flat) shape is called a perimeter. To determine the perimeter of squares, rectangles, or parallelograms, simply add up the total length of the four sides.”



WRITE “ $P = S1 + S2 + S3 + S4$ ” on the flip chart.

STATE: “To determine the perimeter of triangles, simply add up the total length of the three sides.”

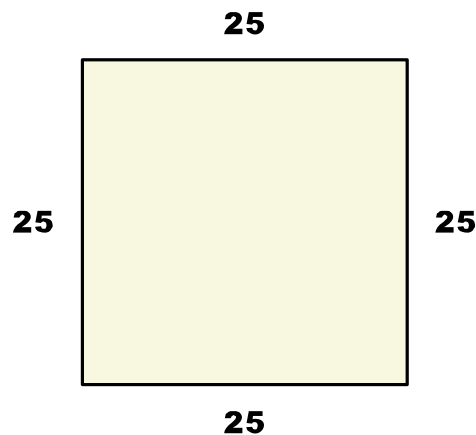


WRITE “ $P = S1 + S2 + S3$ ” on the flip chart.

STATE: “Example 1:”



WRITE the example on the flip chart.



EXPLAIN each step of the process.

Step 1: $P = S1 + S2 + S3 + S4$

Step 2: $P = 25 + 25 + 25 + 25$

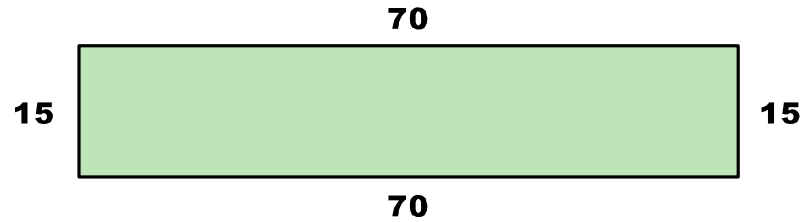
Step 3: $P = 100$



STATE: “Example 2:”



WRITE the example on the flip chart.



EXPLAIN each step of the process.

Step 1: $P = S1 + S2 + S3 + S4$

Step 2: $P = 70 + 15 + 70 + 15$

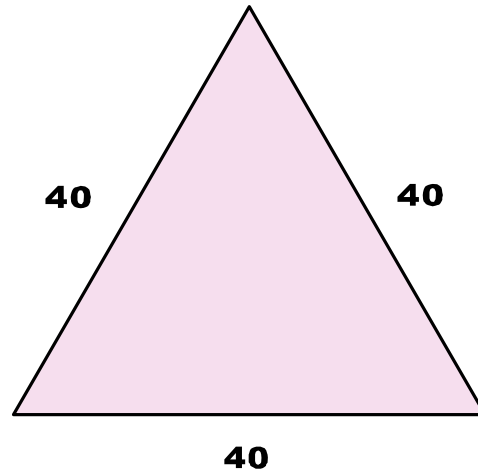
Step 3: $P = 170$



STATE: “Example 3: ”



WRITE the example on the flip chart.



EXPLAIN each step of the process.

Step 1: $P = S1 + S2 + S3$

Step 2: $P = 40 + 40 + 40$

Step 3: $P = 120$



Circumference

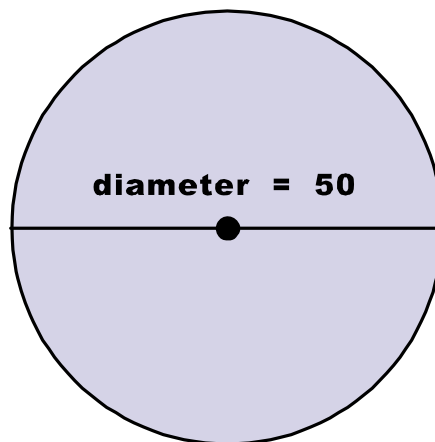
EXPLAIN that the distance around a circle is called its circumference. It has been proven that the circumference of any circle is 3.14 times its diameter. The number 3.14 is referred to as “pi.” To calculate the circumference of a circle, multiply the diameter times pi.

STATE: “Pi is actually a much longer number (3.141592+). It is usually shortened for ease of calculation.”

STATE: “Example 1: ”



WRITE the example on the flip chart.



EXPLAIN each step of the process.

Step 1: $C = \pi d$

Step 2: $C = 3.14 \times 50$

Step 3: $C = 157$



Area

STATE: “Area is the amount of surface occupied by a shape.”

EXPLAIN that, to determine the area of squares and rectangles, simply multiply the length of one side by the length of an adjacent side.

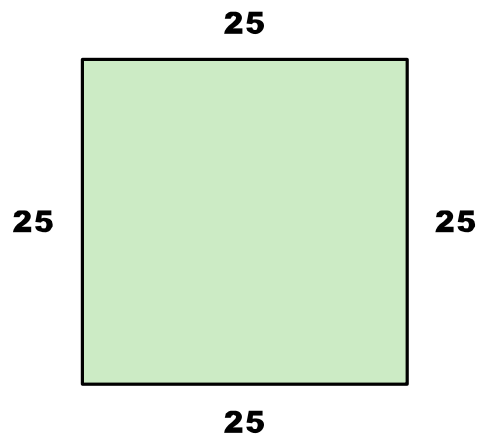


WRITE “ $A = L \times H$ ” on the flip chart.

STATE: “Example 1:”



WRITE the example on the flip chart.



EXPLAIN each step of the process.

Step 1: $A = L \times H$

Step 2: $A = 25 \times 25$

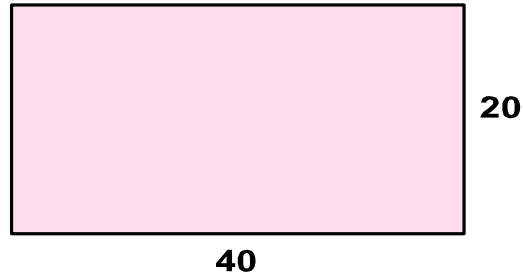
Step 3: $A = 625$



STATE: “Example 2:”



WRITE the example on the flip chart.



EXPLAIN each step of the process.

Step 1: $A = L \times H$

Step 2: $A = 20 \times 40$

Step 3: $A = 800$



EXPLAIN that, to determine the area of a right triangle, multiply the lengths of the sides adjacent to the right angle and divide by two

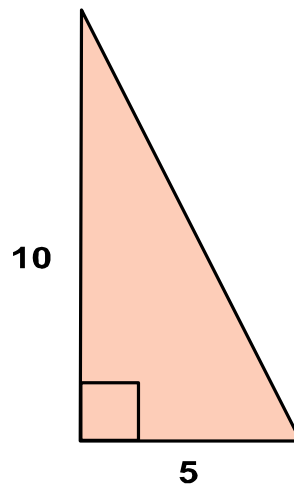


WRITE " $A = (L \times H)/2$ " on the flip chart.

STATE: "Example:"



WRITE the example on the flip chart.



EXPLAIN each step of the process.

Step 1: $A = (L \times H) / 2$

Step 2: $A = (5 \times 10) / 2$

Step 3: $A = 25$

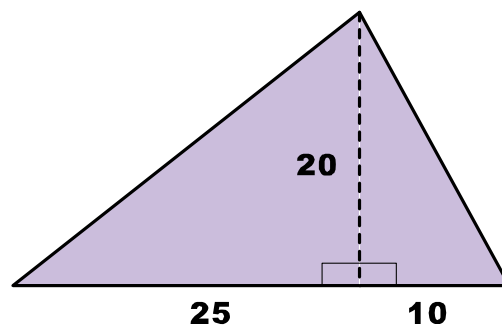


EXPLAIN that, to determine the area of any other triangle, draw an imaginary line through the triangle to form two right triangles. Calculate the area of the “new” right triangles and add them together.

STATE: “Example:”



WRITE the example on the flip chart.



EXPLAIN each step of the process.

Step 1: $A = (L \times H) / 2 + (L \times H) / 2$

Step 2: $A = (10 \times 20) / 2 + (25 \times 20) / 2$

Step 3: $A = 100 + 250$

Step 4: $A = 350$

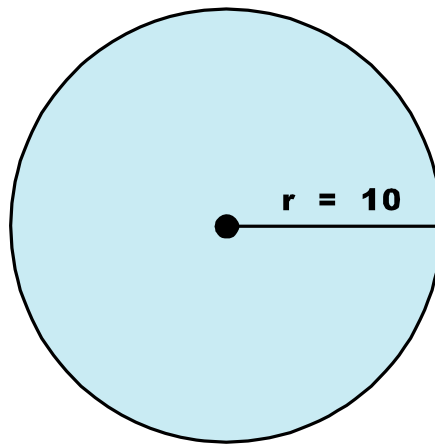


EXPLAIN that, to determine the area of a circle, we will again use pi. It has been proven that the area of a circle is equal to the radius times itself (“r” squared or r^2) times pi.

STATE: “Example:”



WRITE the example on the flip chart.



EXPLAIN each step of the process.

Step 1: $A = \pi r^2$

Step 2: $A = 3.14 \times (10)^2$

Step 3: $A = 3.14 \times 100$

Step 4: $A = 314$

Progress Check #8

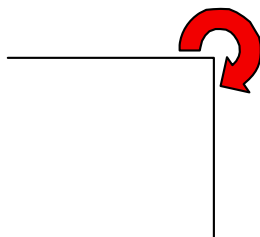


DIRECT the participants to the section titled “Progress Check # 8” in their Participant Guide.

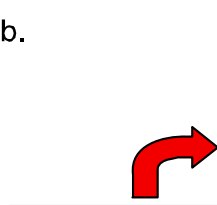
ALLOW them enough time to complete the Progress Check and then review the answers.

- Identify the measure of each of the following angles.

a.



b.

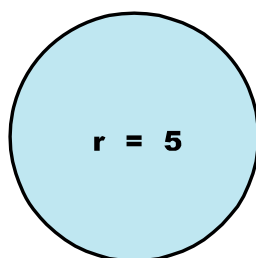


a. 270°

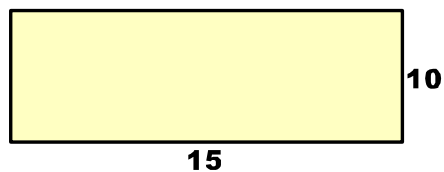
b. 90°

- Calculate the following perimeters:

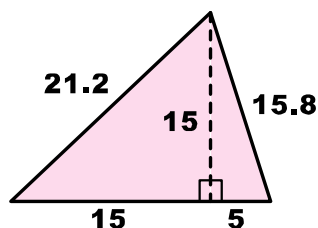
a.



b.



c.



a. 31.4

b. 80

c. 57



3. Calculate the areas for the above shapes.
 - a. 78.5
 - b. 300
 - c. 150

4. If one wall of your rectangular warehouse is 350 feet long and the other wall is 175 feet long, what is the area?
 $61,250 \text{ ft}^2$



Summary



DIRECT the participants to the section titled “Summary” in their Participant Guides.

STATE: “In this module we have covered basic arithmetic with whole numbers and decimals. We have worked with fractions and percentages. We looked at the two measuring systems (standard and metric). We saw how graphs were used. Lastly, we discussed angles and shapes.”

CONCLUDE BY SAYING that, as you have seen, mathematics is crucial to the operation of a warehouse. From determining the number of items received to calculating the area needed for storage, working with numbers is an everyday necessity for inventory management. Understanding how to use mathematics in the workplace will not only make your job easier, but it will help you achieve your career goals.